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# NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

TECHNICAL NOTE

No. 1200

TENTATIVE TABLES FOR THE PROPERTIES  
OF THE UPPER ATMOSPHERE

By Calvin N. Warfield

for the

NACA Special Subcommittee on the Upper Atmosphere

Langley Memorial Aeronautical Laboratory  
Langley Field, Va.



Washington

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## SUMMARY

As a result of recent developments in aeronautics and ordnance, a need has arisen for tables of properties of the atmosphere at altitudes in excess of those covered by the existing standard tables (NACA Report No. 218). In order to satisfy this need, the National Advisory Committee for Aeronautics has adopted three temperature-height relationships and one composition-height relationship, and tables based upon them have been prepared for pertinent properties of the upper atmosphere (that is, from 20 to 120 kilometers in metric units, and from 65,000 to 393,700 feet in British units). In the absence of direct data, such as might be obtained by soundings with high-altitude rockets, the values adopted are based upon existing information obtained by indirect measurements of certain quantities. As a consequence, the tables are only tentative.

Two sets of tables based upon the adopted tentative standard specifications for the upper atmosphere are presented. One set of two tables is based upon the same arbitrary constant value for the acceleration of gravity as was used in the preparation of the existing standard tables for the lower levels (NACA Report No. 218). This set of tables for the upper levels of the atmosphere therefore constitutes a consistent extension of the existing standard tables. The other set of two tables takes into consideration the decrease in the acceleration of gravity with increasing altitude and therefore is more precise than the first set. Consequently, this set is presented only to satisfy the need for greater accuracy that may exist in some fields of research.

Each table is divided into separate parts for both day and night conditions at altitudes above 80 kilometers. The necessity for separate tables for day and night values is occasioned by the

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In April 1946 this Panel was superseded by the Special Subcommittee on the Upper Atmosphere which was also appointed by the NACA.

The membership of this Special Subcommittee is as follows:

~~Dr. Harry Hall - Navy~~  
~~Dr. Joseph Kaplan, C.I.T.~~  
Dr. Harry Wexler, U. S. Weather Bureau, Chairman  
Col. D. N. Yates, Chief, Air Weather Service  
Col. Paul H. Dane, A. C., TSEAC, AAF Air Materiel Command  
Capt. H. T. Orville, USN, Office of Chief of Naval Operations,  
Navy Department  
Capt. Walter S. Diehl, USN, Bureau of Aeronautics, Navy  
Department

^.-Dr. Calvin N. Warfield, Langley Memorial Aeronautical Laboratory  
Dr. E. H. Krause, Naval Research Laboratory  
Dr. W. G. Brombacher, National Bureau of Standards  
Dr. L. V. Berkner, Carnegie Institution of Washington  
Dr. B. Gutenberg, California Institute of Technology  
Dr. Fred L. Whipple, Harvard Observatory, Harvard University  
Dr. O. R. Wulf, Gates and Crellin Laboratories, California  
Institute of Technology.  
Mr. Jerome Teplitz, NACA, Secretary.

This Subcommittee has considered the information available concerning temperature and composition in the upper atmosphere. On the basis of existing data obtained by balloons at altitudes up to about 32 kilometers (references 6 and 7), of indirect measurements obtained at greater heights such as those discussed in references 8 to 14, and of unpublished data resulting from similar indirect measurements, recommendations concerning temperature-height and composition-height relationships were made by the Subcommittee on June 24, 1946. The recommendations regarding temperature-height relationships cover three arbitrary sets of temperature: (1) tentative standard temperatures, (2) probable minimum temperatures, and (3) probable maximum temperatures. Also, recommendation was made that at this time no tables be prepared for altitudes in excess of 120 kilometers because of the uncertainty regarding the validity of the data in this region.

At a meeting of the executive committee of the National Advisory Committee for Aeronautics held on August 15, 1946, the previously mentioned recommendations of the Subcommittee were adopted. As a result of the adoption of the recommendations of the Subcommittee, two sets of tables for the upper atmosphere, based upon the tentative standard temperatures, have been prepared at the Langley Laboratory of the NACA.

The first set of tables provides a consistent extension of the present standard tables for the lower levels of the atmosphere

(reference 1) because the same simplifying assumption of an arbitrary constant value for the acceleration of gravity is made in both cases. Because of this consistency with the present standard atmosphere tables, and in consideration of the fact that the present standard tables (reference 1) are widely used in evaluating performance characteristics of aircraft and for design purposes, it appears that this first set of tables may also be found useful in these same fields of aeronautical engineering. In addition, in order to be consistent with present practice in the use of the terms "pressure altitude" and "density altitude" (reference 15) it appears that it may be proper to use the term "tentative pressure altitude" to designate that altitude in this first set of tables which corresponds to a specified ambient-air pressure. Likewise, the term "tentative density altitude" can consistently be used with this set of tables in connection with ambient-air densities.

The second set of tables is more precise than the first because it takes into consideration the decrease in the acceleration of gravity with increasing altitude. This set is intended primarily for use in connection with research on the properties of the upper atmosphere. Values of still greater computational precision than those listed in this second set may be obtained by means of "latitude correction factors" which have been computed and tabulated in another table.

These two sets of tables for the upper atmosphere consist of two tables each, one in the metric system of units and the other in the British system of units. The altitude range covered is from 20 kilometers and 65,000 feet, respectively, to 120 kilometers and its British equivalent of about 393,700 feet. In addition to those quantities reported in references 1 to 5, there is included the mean free path of the air molecules. This quantity has been added because of its significance at high altitudes where the molecular mean free paths may be comparable to or larger than certain dimensions of the aircraft or missiles that may be flown there.

Acknowledgement is gratefully given for the contributions made by Dr. R. G. Stone, of the AAF Weather Service, who supplied valuable data concerning maximum and minimum temperatures over the entire world to altitudes of 32 kilometers, and for the thorough technical review and excellent suggestions offered by Mr. L. P. Harrison of the U. S. Weather Bureau.

## SYMBOLS

a	speed of sound
c	most probable molecular speed
$\bar{c}$	average molecular speed
g	acceleration of gravity
h	altitude
K	volume gradient of oxygen dissociation $\left(\frac{\Delta v}{\Delta h}\right)$
L	temperature gradient $\left(\frac{\Delta T}{\Delta h}\right)$
M	molecular weight
m	mass of a molecule
N	number of molecules per unit volume
p	pressure
R	universal gas constant
r	radius of the earth
T	absolute temperature
t	temperature
v	volume of molecular oxygen in an initial unit volume of normal air, at the same temperature and pressure
w	specific weight (go)
$\gamma$	ratio of specific heats

$\lambda$	mean free path of molecules
$\mu$	coefficient of viscosity
$\nu$	kinematic viscosity ( $\mu/\rho$ )
$\rho$	density (mass per unit volume)
$\sigma$	molecular diameter; also density ratio ( $\rho/\rho_0$ )
$\bar{\sigma}$	average molecular diameter

The following subscripts are used to refer to the indicated conditions:

O	sea level
l	lower level
a	top of region of dissociation, where oxygen is all atomic
A	base of region with constant temperature and constant composition
B	base of region with constant temperature gradient and constant composition
C	base of region with constant temperature and constant volume gradient of dissociation
D	base of region with constant temperature gradient and constant volume gradient of dissociation
g	acceleration of gravity variable
m	base of region of dissociation, where oxygen is all molecular
n	nitrogen molecules
N	non-oxygen (i. e., all constituents other than oxygen)
o	oxygen
air	mixture of molecules in atmosphere
$\phi$	latitude

## ADOPTED SPECIFICATIONS FOR THE UPPER ATMOSPHERE

## Tentative Temperatures

Three sets of tentative temperature-height relationships have been adopted. One set gives tentative standard temperatures and the other two list values of the probable minimum and the probable maximum temperatures for the entire world. These three sets of temperatures which were originally recommended by the Subcommittee on the Upper Atmosphere are given by linear variations with altitude between the points specified in the following tabulation of temperatures.

## TEMPERATURES

Altitude (km)	Probable minimum (°K) (a)	Tentative standard (°K)	Probable maximum (°K) (a)
0	225	b <sub>288</sub>	320
10.76923		b <sub>218</sub>	
11			250
17	180		
20		b <sub>218</sub>	
25			255
32		218	
45	200		380
50		350	
55	300		
60		350	
70			380
78		240	
80	170		300
83		240	
120	300	375	600

<sup>a</sup>The values of ambient air temperature listed in these two columns are not intended to represent extreme values for the entire world, and for all time, but rather values that bracket the temperatures over nearly all the earth most all the time.

<sup>b</sup>These values are standard, and have been used previously in references 1, 3, 4, and 5.

These temperature-altitude relationships are also shown in figure 1.



### Tentative Composition

The tentative composition used in computing the tables was arrived at by taking into consideration the fact that, at altitudes below 80 kilometers in the day time and below 105 kilometers at night, the generally accepted variations in chemical composition are too small to affect appreciably the computed pressures and densities. However, it is believed that at levels above those just specified significant changes in composition result from the dissociation of oxygen molecules by solar radiation. It is furthermore known that the presence of water vapor in the atmosphere does not appreciably affect pressures and densities. As a result of such considerations, and in the interest of simplicity, the following tentative specifications for composition of the upper atmosphere were recommended by the Subcommittee and have been adopted for the purposes of computing the values in these tables:

(1) For day time, the dissociation of oxygen is such as to produce a linear volume gradient from all-molecular oxygen at 80 kilometers to all-atomic oxygen at 100 kilometers. Except for oxygen dissociation, the composition is the same as that at sea level.

(2) For night time, the dissociation of oxygen is such as to produce a linear volume gradient from all-molecular oxygen at 105 kilometers to all-atomic oxygen at 120 kilometers. Except for oxygen dissociation the composition is the same as that at sea level.

(3) At altitudes below the regions of oxygen dissociation the composition is the same as that at sea level.

(4) At altitudes above the regions in which both molecular and atomic oxygen exist, as stipulated in (1) and (2), and up to at least 120 kilometers, the composition is the same as that at sea level, except for oxygen which is in the atomic rather than in the molecular form.

The variation with altitude of the specified molecular oxygen content of the atmospheres is graphically portrayed in figure 2.

### PHYSICAL RELATIONSHIPS

#### Basic Equations

In addition to the specifications for temperature and composition already listed, certain other assumptions are made and

serve as the basis for deriving the various equations used in computing the properties of the upper atmosphere. These additional assumptions are:

(a) The air is dry

(b) The air behaves as a perfect gas and hence obeys the general gas law which may be written

$$\frac{\rho}{\rho_0} = \frac{p}{p_0} \frac{T_0}{T} \frac{M}{M_0} \quad (1)$$

(c) The air is at rest with respect to the earth and hence obeys the basic law for fluid statics

$$dp = -g_0 dh \quad (2)$$

By means of equations (1) and (2) and equations representing the adopted specifications for temperature and composition, relationships may be deduced between pressure and height. The equations representing the adopted specifications are

$$T = T_1 + L(h - h_1) \quad (3)$$

where  $L$  is the temperature gradient  $\Delta T/\Delta h$ , and

$$\frac{M}{M_0} = \frac{1}{1 - K(h - h_m)} \quad (4)$$

where  $K$  is the volume gradient of oxygen dissociation  $\Delta v/\Delta h$ . The derivation of equation (4) is given in appendix A.

In addition to the three assumptions just listed, it is necessary to make an assumption concerning the value of the acceleration of gravity. For the purpose of furnishing tables for the upper atmosphere that will be consistent with the present standard tables for the lower atmosphere (reference 1), it is necessary to make the same assumption concerning the acceleration of gravity as was used in preparing the standard tables. This assumption is

(d) For the tables based on a constant value of  $g$  the acceleration of gravity at all altitudes is the standard sea-level value; that is,

$$g = g_0 \quad (5)$$

For those instances in which closer conformity to actual conditions is required than is inherent in these tables it is necessary to make another assumption concerning the value of the acceleration of gravity. This assumption is

- (e) For tables based on a variable value of  $g$  the acceleration of gravity varies inversely as the square of the distance from the center of the earth; that is,

$$g = g_0 \left( \frac{r}{r + h} \right)^2 \quad (6)$$

#### Pressure-Height Relationships

By use of the foregoing basic equations and assumptions, other equations are derived which relate pressure to altitude. Two sets of equations are used, one set based on a constant value of  $g$  as specified in assumption (d), the other set based on the variation of  $g$  that is specified in assumption (e). The deductions for the first set are indicated in appendix B and for the second set in appendix C. The equations that are based on a constant value of  $g$  are as follows:

For combination A (constant temperature and constant composition):

$$\log_e \left( \frac{p}{p_A} \right) = C_A (h - h_A) \quad (7)$$

where

$$C_A = - \frac{g_0 \rho_0}{p_0} \frac{T_0}{T} \frac{M}{M_0} \quad (8)$$

For combination B (constant temperature gradient and constant composition):

$$\log \left( \frac{p}{p_B} \right) = C_B \log \left( \frac{T}{T_B} \right) \quad (9)$$

where

$$C_B = - \frac{g_0 \rho_0 T_0}{p_0 L} \frac{M}{M_0} \quad (10)$$

For combination C (constant temperature and constant volume gradient of dissociation):

$$\log \left( \frac{p}{p_C} \right) = C_C \log \left( \frac{M}{M_C} \right) \quad (11)$$

where

$$C_C = - \frac{E_0 p_0 T_0}{p_0 K T} \quad (12)$$

For combination D (constant temperature gradient and constant volume gradient of dissociation):

$$\log \left( \frac{p}{p_D} \right) = C_D \log \left( \frac{T}{T_D} \frac{M}{M_D} \right) \quad (13)$$

where

$$C_D = \frac{-E_0 p_0 T_0 M_D}{p_0 (M_0 + M_D T_D K)} \quad (14)$$

The equations derived in appendix C, based on a variable value of  $g$ , are more complex than those listed in the foregoing and consequently they are not reproduced here.

#### Speed of Sound

The speed of sound at any altitude relative to that at sea level is computed by the equation

$$\frac{a}{a_0} = \left( \frac{\gamma T M_0}{\gamma_0 T_0 M} \right)^{1/2} \quad (15)$$

where the ratio of the specific heats  $\gamma$ , as derived in appendix A, is

$$\frac{\gamma}{\gamma_0} = 1 - \frac{128K(h - h_m)}{21M_0} \quad (16)$$

The variation with altitude of the ratio of specific heats  $\gamma$  for the specified atmosphere is shown in figure 3(a).

#### Coefficient of Viscosity

Sutherland's equation for the variation of the coefficient of viscosity with temperature is used. It is

$$\frac{\mu}{\mu_0} = \left( \frac{T}{T_0} \right)^{3/2} \left( \frac{T_0 + S}{T + S} \right) \quad (17)$$

in which, according to reference 16,

$$S = 120$$

when the  $T$ 's are in  $^{\circ}\text{K}$ , and

$$S = 216$$

when the  $T$ 's are in  $^{\circ}\text{F}$  absolute.

A caution concerning the use of values obtained from equation (17) for the upper atmosphere is given in the section entitled "Discussion of Tables."

#### Molecular Mean Free Path

The ratio of the molecular mean free path at any altitude to the corresponding value at sea level is computed by

$$\frac{\lambda}{\lambda_0} = \frac{p_0 T g}{p T_0 g_0} \quad (18)$$

This equation is justified in appendix D.

#### BASIC CONSTANTS

In the preceding section equations are given by means of which several properties of the upper atmosphere are computed. These computations involve numerical values of the several properties at sea level. Appendix E discusses the chosen sea-level values for

each of several properties of the atmosphere and they are listed in table I in both metric and British engineering systems of units. Values are listed for each of the three specified atmospheres and in some instances the quantity is expressed in more than one unit in either the metric or British system.

The values listed in table I for the standard atmosphere at sea level are identical with those used in references 1 and 5 except in a few instances. The exceptions are noted and explained in appendix E.

#### DISCUSSION OF TABLES

The appropriate equation (equation (7), (9), (11) or (13) for the constant value of  $g$ , or (C3), (C6), (C10) or (C13) for the variable values of  $g$ ) is used to compute the ratio of the pressure  $p$  at any height to the pressure at the base of the region to which that particular equation applies. These pressure ratios for each of the regions are then used to compute the ratio of the pressure  $p$  to the pressure  $p_0$  at sea level. These ratios  $p/p_0$  are given in tables II to V.

By use of the computed values of the pressure ratios  $p/p_0$  and of the sea-level value of pressure  $p_0$  as given in table I, the value of the pressure  $p$  is computed and then given in tables II to V. The pressures given in tables IV and V are also plotted against altitude in figure 3(b).

The remaining quantities given in tables II to V are similarly computed by means of the appropriate equation and the corresponding sea-level value given in table I. The values for these remaining quantities given in tables IV and V are also shown plotted against altitude in figures 3(c) to 3(h).

Attention is directed to the fact that all tables in this report are based on the engineering system (sometimes referred to as the gravitational system) in which the fundamental quantities are length, force, and time. The standard units for force used herein are, therefore, pounds for the British system and kilograms for the metric system.

### Accuracy of Computed Tables II to V

In tables II to V all quantities except the mean free paths of the molecules are tabulated to four significant figures, and the mean free paths of the molecules are tabulated to three significant figures. All computations for table II were carried through to six significant figures and consequently the values given in this table are believed to be exact.

Most of the values for table IV were obtained from table II by use of suitable conversion factors evaluated by a graphical method described in appendix C. The errors resulting from the method, and therefore the errors in the values tabulated in table IV are believed not to exceed 0.01 of 1 percent.

A method of graphical interpolation was applied to obtain from tables II and IV the values for use at the intermediate levels tabulated in tables III and V. The accuracy of this method is such as to introduce an error of not over one-twentieth of 1 percent in the values listed in tables III and V. Consequently, whenever a discrepancy exists between the metric and British values, the metric values should govern.

### Validity of Tabulated Values at the Higher Altitudes

Pressure, density, specific weight, and mean free path of molecules. - As was previously mentioned, the computations for tables II and III are based on a constant value for the acceleration of gravity  $g$  so that the values listed would be consistent with those appearing in the present standard tables for the lower levels of the atmosphere (reference 1). The errors in the computed values of pressure, density, specific weight and mean free path inherent in the assumption of a constant value for the acceleration of gravity become progressively greater with increasing altitude, being about 30 percent at 120 kilometers. However, a variation of 30 percent in pressure at 120 kilometers corresponds to a variation of less than 4 percent in altitude at this level, and at lower levels the change in altitude corresponding to the error in pressure rapidly approaches zero. It is apparent therefore that in at least some applications the values in tables II and III will be adequate and therefore useful. Furthermore, they represent an extension of the present standard tables (reference 1).

In order to satisfy the need that may exist for values that are not affected by the use of a constant value for the acceleration of gravity  $g$ , tables IV and V are presented. In these tables  $g$  is assumed to vary inversely as the square of the

distance from the center of the earth. This assumption therefore takes into consideration the variation due to gravitational attraction, but it does not allow for the effect of centrifugal force. The centrifugal force due to the rotation of the earth is known to be only a small fraction of 1 percent of the gravitational force at an altitude of 120 kilometers, and consequently this omission does not result in a significant error.

The standard value used for the acceleration of gravity at sea level (and at all altitudes for tables II and III) is 9.80665 meters per second per second. This value corresponds rather closely to the true acceleration of gravity at sea level at latitude  $45^\circ$ . (More specifically, it corresponds to the theoretical acceleration of gravity at sea level and at latitude  $45^\circ 24'$  according to the International formula. See reference 17.) If still greater accuracy than is inherent in tables IV and V is required at latitudes far displaced from latitude  $45^\circ$ , an estimate of the latitude effect upon pressure and density may be obtained by use of the equation

$$\log \frac{p_\phi}{p_0} = \frac{g_{0\phi}}{g_0} \log \frac{p}{p_0} \quad (19)$$

where  $p_\phi$  is the pressure at altitude  $h$  and at latitude  $\phi$ , and  $g_{0\phi}$  is the acceleration of gravity at sea level and at latitude  $\phi$ . A similar equation (replacing  $p$ 's with  $\rho$ 's) applies to densities.

By means of equation (19) it can be shown that a latitude correction factor (L.C.F.) defined by

$$\text{L.C.F.} = \frac{p_\phi}{p} \quad (20)$$

can be computed by

$$\text{L.C.F.} = \left( \frac{p}{p_0} \right)^{\frac{g_{0\phi} - g_0}{g_0}} \quad (21)$$



If values of  $g_0$  from reference 17 are used, the following values for the exponent  $(g_0 - g_0)/g_0$  are obtained:

Latitude (deg)	$\frac{g_0 - g_0}{g_0}$	Latitude (deg)	$\frac{g_0 - g_0}{g_0}$
0	$-2.66758 \times 10^{-3}$	50	$0.42175 \times 10^{-3}$
10	-2.50922	60	1.28372
20	-2.05299	70	1.98732
30	-1.35337	80	2.44701
40	-0.49405	90	2.60670

The foregoing exponents when applied to the values of pressure ratio  $p/p_0$  tabulated in tables IV and V give the values of the latitude correction factor described by equations (20) and (21). For latitudes at increments of  $10^\circ$  and for altitudes at increments of 10 kilometers the latitude correction factors that are applicable to the pressures given in tables IV and V have been computed and are presented in table VI. By means of table VI it is therefore possible to obtain computed values of pressure which take into consideration the variation with latitude of the sea-level value of the acceleration of gravity  $g_0$ . This computation may be made by use of equation (20) which may be written  $p_0 = (L.C.F.) p$ .

Coefficient of viscosity and kinematic viscosity. - The Sutherland formula (equation (17)) is strictly applicable only to a gas of constant composition and to pressures which are not too small, and consequently the tabulated values for the coefficient of viscosity and for the kinematic viscosity are obviously not entirely reliable at the higher altitudes. However, the lack of data on the viscosity of oxygen in the atomic form does not permit at this time an estimation of the correction that is needed to allow for the specified dissociation. Furthermore, because of the fact that the effective value of the viscosity of a gas at very low pressure flowing over a body depends on the size and shape of the body, it is not practical to give a correction that will be applicable to more than one specific size and shape of a body. The values for viscosity at the higher altitudes should therefore be used with caution.

Speed of sound. - The tabulated values for the speed of sound are believed to be correct for all altitudes covered by the tables.

Caution should be exercised, however, in using the tabulated values for the upper altitudes in connection with Mach numbers because at high altitudes where the mean free paths of the air molecules are large in comparison with the dimensions of the body moving through them, the laws of fluid dynamics do not apply and the laws of particle dynamics must be used. When aerodynamic forces, for example, are computed for these conditions by use of the laws of particle dynamics the most probable speed of the air molecules is found to be the basic quantity rather than the speed of sound.

As in the case of viscosity, the altitude range in which the most probable speed of the air molecules replaces the speed of sound as the basic quantity depends upon the size of the body under consideration. It is consequently not possible to specify a single level at which the molecular speed becomes significant in aerodynamics. For this reason values for the speed of sound are listed to 120 kilometers.

In any case in which the most probable speed of the air molecules  $c$  is needed rather than the velocity of sound  $a$  it is possible to obtain the value of  $c$  from the value of  $a$  listed in the tables by use of the appropriate factor obtained from the following tabulation:

Altitude, h		Ratio of the most probable molecular speed to the speed of sound, $\frac{c}{a} = \sqrt{\frac{2}{\gamma}}$	
(m)	(ft)	Day	Night
80,000	262,467	1.195	1.195
85,000	278,871	1.189	1.195
90,000	295,275	1.183	1.195
95,000	311,679	1.176	1.195
100,000	328,083	1.170	1.195
105,000	344,487	1.170	1.195
110,000	360,892	1.170	1.187
115,000	377,296	1.170	1.179
120,000	393,700	1.170	1.170

#### CONCLUDING REMARKS

The fact should be emphasized that the values given in the tables for the upper atmosphere are only tentative and as such may become obsolete after a sufficient number of reliable direct

measurements of certain quantities have been made available. In the meantime these tentative tables should be useful not only in serving as a basis for comparing performance characteristics and estimating limiting values of performance, but also in securing the additional data needed for revising these tentative tables for the upper atmosphere.

Langley Memorial Aeronautical Laboratory  
National Advisory Committee for Aeronautics  
Langley Field, Va., December 6, 1946

## APPENDIX A

## VARIATION WITH ALTITUDE OF MOLECULAR WEIGHT

## AND RATIO OF SPECIFIC HEATS

## Molecular Weight in the Region of Oxygen Dissociation

Consider an initial unit volume of normal air composed only of molecular gases, consisting of oxygen and other constituents. Let all the non-oxygen constituents be diatomic of average molecular weight  $M_N$ , and let the molecular weight of oxygen in the molecular form be  $M_m$ , and in the atomic form  $M_a$ . Then

$$M_a = \frac{1}{2} M_m \quad (A1)$$

Let the initial conditions be as follows:

$v_0$  volume of all-molecular oxygen at height  $h_m$

$1 - v_0$  volume of non-oxygen components at height  $h_m$

$M_0$  average molecular weight of the initial air mixture at height  $h_m$

Then

$$M_0 = v_0 M_m + (1 - v_0) M_N \quad (A2)$$

At height  $h$ , between  $h_m$  and  $h_a$  (where  $h_m$  is height at base of region in which dissociation occurs, and  $h_a$  is height at top of the region, and where all the oxygen is in the atomic form) the volume of molecular oxygen  $v_m$  per unit initial volume of normal air is

$$v_m = v_0 \left( \frac{h_a - h}{h_a - h_m} \right) \quad (A3)$$

and the volume of atomic oxygen  $v_a$  per unit initial volume of normal air is

$$v_a = 2v_0 \left( \frac{h - h_m}{h_a - h_m} \right) \quad (A4)$$

Therefore, the average molecular weight  $M$  of the atmosphere at height  $h$  can be shown to be

$$M = \frac{M_0}{1 - K(h - h_m)} \quad (A5)$$

where

$$K = - \frac{v_0}{h_a - h_m} \quad (A6)$$

the volume gradient of molecular oxygen,  $\Delta v/\Delta h$ .

#### Ratio of Specific Heats in the Region of Oxygen Dissociation

The ratio of specific heats  $\gamma$  for diatomic gases is taken to be 7/5 and for monatomic gases, 5/3. If the ratio of the specific heats  $\gamma$  for the atmosphere is assumed to be given by a weighted average, according to relative masses, of the values of  $\gamma$  for diatomic and monatomic gases, it can be shown, by using equations (A1), (A2), (A3), and (A4) that for those regions of the atmosphere in which dissociation of oxygen occurs

$$\gamma = \frac{7}{5} + \frac{4}{15} v_0 \left( \frac{M_m}{M_0} \right) \left( \frac{h - h_m}{h_a - h_m} \right) \quad (A7)$$

The standard value for  $\gamma_0$ , for the atmosphere at sea level, is 7/5, and for  $M_m$  the standard value is 32. Therefore

$$\frac{\gamma}{\gamma_0} = 1 - \frac{128K(h - h_m)}{21M_0} \quad (A8)$$

It is estimated that in the tentative standard atmosphere the variation of  $\gamma$  due to pressure and temperature effects is only about 0.6 of 1 percent. For this reason the effect of pressure and temperature upon  $\gamma$  is ignored in computing these tentative tables.

## APPENDIX B

VARIATION OF PRESSURE WITH ALTITUDE (ASSUMING THE  
ACCELERATION OF GRAVITY IS A CONSTANT  $g_0$ )

The equations relating atmospheric pressure to height for all altitude ranges in all three atmospheres (minimum, standard, and maximum temperatures) are only four in number. These four equations represent all possible combinations of the two types of temperature-height relationship and the two types of composition-height relationship. The deductions of the equations are based upon the familiar hydrostatic relation

$$dp = - g_0 \rho \, dh \quad (B1)$$

and upon the general gas equation

$$\frac{\rho}{\rho_0} = \frac{p}{p_0} \frac{M}{M_0} \frac{T_0}{T} \quad (B2)$$

These two equations, when combined, give

$$\frac{dp}{p} = - \frac{g_0 \rho_0 T_0 M \, dh}{p_0 T M_0} \quad (B3)$$

The differential equation (B3) is then used for deriving algebraic equations for pressure as a function of altitude, for each of the four combinations of temperature-height and composition-height relationships previously discussed. The derivations are indicated in the following paragraphs and the resulting equations are used in the preparation of tables II and III.

Combination A (constant temperature and constant composition).--  
The type of atmosphere in which both the temperature and composition are constant may be represented algebraically by

$$T = \text{Constant}$$

and

$$M = \text{Constant}$$

Equation (B3) when integrated between the limits of height  $h_A$  and height  $h$  then becomes,

$$\log_e \left( \frac{p}{p_A} \right) = \frac{-g_0 \rho_0 T_0^M}{p_0 T M_0} (h - h_A) \quad (B4)$$

where  $h_A$  is the base of the region in which type A conditions prevail.

Combination B (constant temperature gradient and constant composition). - For the type of atmosphere having a constant temperature gradient and constant composition, let the temperature gradient be represented by

$$L = \text{Constant} = \frac{\Delta T}{\Delta h} \quad (B5)$$

and the temperature by

$$T = T_B + L(h - h_B) \quad (B6)$$

where  $T_B$  and  $h_B$  are the respective values at the base of the region to which combination B conditions prevail. Also  $M = \text{Constant}$ . Equation (B3) then becomes

$$\frac{dp}{p} = \left( \frac{-g_0 \rho_0 T_0^M}{p_0 M_0} \right) \frac{dh}{T_B + L(h - h_B)} \quad (B7)$$

and when integrated between the limits of  $h_B$  and  $h$  this equation becomes

$$\log \left( \frac{p}{p_B} \right) = - \frac{g_0 \rho_0 T_0^M}{p_0 M_0} \log \left( \frac{T}{T_B} \right) \quad (B8)$$

Combination C (constant temperature and constant volume gradient of dissociation). - In the type of atmosphere where both the temperature and volume gradient of dissociation are constant

$$T = \text{Constant}$$

and an expression for  $M$  as a function of  $h$  is derived in appendix A, and it is found to be

$$M = \frac{M_0}{1 - K(h - h_m)} \quad (B9)$$

where  $K$  is the volume gradient of molecular oxygen defined by

$$K = \frac{\Delta v}{\Delta h} = \text{Constant} \quad (B10)$$

Using these relationships with equation (B3) gives

$$\frac{dp}{p} = - \frac{80\rho_0 T_0 dh}{p_0 T [1 - K(h - h_m)]} \quad (B11)$$

Integrating equation (B11) between the limits of  $h_c$  and  $h$ , where  $h_c$  is the height at the base of the region in which type C conditions prevail, gives

$$\log \left( \frac{p}{p_c} \right) = \frac{80\rho_0 T_0}{p_0 T K} \log \left( \frac{M_c}{M} \right) \quad (B12)$$

Combination D (constant temperature gradient and constant volume gradient of dissociation). - The type of atmosphere having both the temperature gradient and the volume gradient of dissociation constant is referred to as combination D. For this combination, the expression for molecular weight given in equation (B9) and an appropriate modification of equation (B6) give, for equation (B3), the following equation:

$$\frac{dp}{p} = - \frac{80\rho_0 T_0 dh}{p_0 [1 - K(h - h_m)] [T_D + L(h - h_D)]} \quad (B13)$$



Integrating the variable part of the right-hand member, between the limits of  $h_D$  and  $h$ , gives

$$\frac{1}{(1 + Kh_m)L + (T_D - Lh_D)K} \log \frac{T_D + L(h - h_D)}{1 - K(h - h_m)} \Bigg|_{h_D}^h$$

Therefore

$$\log \left( \frac{p}{p_D} \right) = \frac{-g_0 \rho_0 T_0 M_D}{p_0 (M_0 L + M_D K T_D)} \log \left( \frac{T_M}{T_D M_D} \right) \quad (B14)$$

## APPENDIX C

VARIATION OF PRESSURE WITH ALTITUDE (ASSUMING THE ACCELERATION  
OF GRAVITY VARIES INVERSELY AS THE SQUARE OF THE  
DISTANCE FROM THE CENTER OF THE EARTH)

The equations relating pressure and altitude derived herein are based upon the general differential equation derived from equation (B2) of appendix B, from the hydrostatic relation

$$dp = -g \rho dh \quad (C1)$$

and from the equation representing the inverse square variation of the acceleration of gravity

$$g = g_0 \left( \frac{r}{r + h} \right)^2 \quad (C2)$$

This general differential equation is

$$\frac{dp}{p} = \frac{-g_0 \rho_0 T_0 M r^2 dh}{p_0 T M_0 (r + h)^2} \quad (C3)$$

As in appendix B four equations are deduced for use in each of the four possible combinations of specified temperature-altitude and composition-altitude relationships. The resulting algebraic equations are used in the preparation of tables IV and V. The deductions for each combination are indicated in the following paragraphs.

Combination A (constant temperature and constant composition).-

For combination A (constant temperature and constant pressure) the algebraic equation relating pressure and altitude is obtained by integrating equation (C3) between the limits of altitude  $h_A$  and  $h$ . The result is

$$\log_e \left( \frac{p}{p_A} \right)_g = \frac{-g_0 \rho_0 T_0 M}{p_0 T M_0} \frac{r^2 (h - h_A)}{(r + h)(r + h_A)} \quad (C4)$$

(Note that in this equation and succeeding equations the subscript  $g$  is used to indicate values computed with the variation in the acceleration of gravity that is specified by equation (C2).)

Combination B (constant temperature gradient and constant composition).— For combination B (constant temperature gradient and constant composition) the differential equation is obtained by substituting in equation (C3) the value for  $T$  given by

$$T = T_B + L(h - h_B) \quad (C5)$$

The differential equation is then

$$\frac{dp}{p} = \frac{-g_0 \rho_0 T_0 M r^2 dh}{p_0 M_0 [T_B + L(h - h_B)] (r + h)^2} \quad (C6)$$

The algebraic equation obtained by integrating equation (C6) between the appropriate limits is

$$\log_e \left( \frac{p}{p_B} \right)_g = C_{B_g} \left[ \frac{r(h - h_B)}{(r + h)(r + h_B)} + \frac{rL}{rL + h_B L - T_B} \log_e \frac{(r + h)T_B}{(r + h_B)T} \right] \quad (C7)$$

where

$$C_{B_g} = \frac{g_0 \rho_0 T_0 M}{p_0 M_0 \left[ L - \frac{1}{r}(T_B - Lh_B) \right]} \quad (C8)$$

Combination C (constant temperature and constant volume gradient of dissociation).— For combination C (constant temperature and constant volume gradient of dissociation) the differential equation is obtained by substituting in equation (C3) the value of  $M$  given by

$$M = \frac{M_0}{1 - K(h - h_m)} \quad (C9)$$

The differential equation is then

$$\frac{dp}{p} = \frac{-g_0 p_0 T_0 r^2 dh}{p_0 T [1 - K(h - h_m)] (r + h)^2} \quad (C10)$$

The algebraic equation obtained by integrating equation (C10) between appropriate limits is

$$\log_e \left( \frac{p}{p_C} \right)_g = C_{Cg} \left\{ \left[ \frac{K}{K + \frac{1 + Kh_C}{r}} \log_e \frac{M(r + h)}{M_0(r + h_C)} \right] - \frac{r(h_C - h)}{(r + h)(r + h_C)} \right\} \quad (C11)$$

where

$$C_{Cg} = \frac{-g_0 p_0 T_0}{p_0 T \left( K + \frac{1 + Kh_C}{r} \right)} \quad (C12)$$

Combination D (constant temperature gradient and constant volume gradient of dissociation). - For combination D (constant temperature gradient and constant volume gradient of dissociation) the differential equation is obtained by substituting in equation (C3) the values of  $T$  and  $M$  given by a slightly modified form of equation (C5) and by equation (C9), respectively. The resulting differential equation is then

$$\frac{dp}{p} = \frac{-g_0 p_0 T_0 r^2 dh}{p_0 [T_D + L(h - h_D)] [1 - K(h - h_m)] (r + h)^2} \quad (C13)$$

The algebraic equation obtained by integrating equation (C13) between appropriate limits is

$$\log_e \left( \frac{p}{p_D} \right)_g = C_{Dg} \left[ \frac{a(h - h_D)}{(1 + xh)(1 + xh_D)} + \frac{b}{x} \log_e \left( \frac{1 + xh}{1 + xh_D} \right) + \frac{c}{y} \log_e \left( \frac{1 + yh}{1 + yh_D} \right) + \frac{d}{z} \log_e \left( \frac{1 + zh}{1 + zh_D} \right) \right] \quad (C14)$$

where

$$C_{Dg} = \frac{-g_0 p_0 T_0}{p_0 (T_D - Lh_D) (1 + Kh_m)} \quad (C15)$$

$$x = \frac{1}{r}$$

$$y = \frac{L}{(T_D - Lh_D)}$$

$$z = \frac{-K}{(1 + Kh_m)}$$

$$a = \frac{x^2(x^2 + yz - yx - zx)}{(z - x)^2(y - x)^2}$$

$$\frac{b}{x} = \frac{x(2yz - xy - xz)}{(z - x)^2(y - x)^2}$$

$$\frac{c}{y} = \frac{-y^2}{(y - x)^2(z - y)}$$

$$\frac{d}{z} = \frac{z^2}{(z - x)^2(z - y)}$$

Equations (C4), (C7), (C11), and (C14) were used to compute the pressure ratios at the transition levels only in the tentative standard atmosphere. By dividing these pressure ratios by the pressure ratios at the same transition levels obtained by use of the equations in appendix B based on a constant value for the acceleration of gravity, a conversion factor was obtained for each of the several transition altitudes. Since it was impractical to use these complex equations for directly computing the pressure

ratios at all the levels recorded in tables IV and V, the values at these numerous intermediate levels were arrived at as follows:

(1) For each altitude a value for the conversion factor was computed by algebraic summation from the equation

$$\log_e \left( \frac{p_g}{p} \right) = \frac{\rho_0 T_0}{\rho_0 M_0} \sum_0^h (g_0 - g) \frac{M}{T} \Delta h \quad (C16)$$

where  $p_g$  is the pressure based on the variable value of  $g$ , and  $p$  is the pressure based on a constant value for the acceleration of gravity. In equation (C16) the proper value of  $g$ ,  $T$ , and of  $M$  was substituted for each region of the atmosphere, according to equation (C2), (C5), and (C9), respectively.

(2) The values of  $p_g/p$  so computed were plotted against altitude to define the shape of the curve relating pressure ratios to altitude.

(3) The accurate values for the pressure ratio computed by equations (C4), (C7), (C11), and (C14) and by equations (B4), (B8), (B12), and (B14) were also plotted and another curve was drawn through these points representing the accurately computed ratios and faired according to the curve drawn through the points obtained by use of equation (C16).

(4) The curve arrived at from step (3) was then used to obtain conversion factors for each of the altitudes recorded in tables IV and V.

## APPENDIX D

## MOLECULAR MEAN FREE PATHS

## Ratio of the Mean Free Paths of Molecules

The conventional equation for the mean free path of the molecules  $\lambda$  of a gas (reference 18) is

$$\lambda = \frac{1}{\pi \sqrt{2} N \sigma^2} \quad (D1)$$

Therefore the ratio of the mean free path at any altitude to the value at sea level is

$$\frac{\lambda}{\lambda_0} = \frac{N_0}{N} \left( \frac{\sigma_0}{\sigma} \right)^2 \quad (D2)$$

But

$$Nm = \rho \quad (D3)$$

and

$$g\rho = \frac{pM}{RT} \quad (D4)$$

Therefore

$$\frac{N_0}{N} = \frac{p_0}{p} \frac{T}{T_0} \frac{g}{g_0} \quad (D5)$$

and

$$\frac{\lambda}{\lambda_0} = \frac{p_0}{p} \frac{T}{T_0} \frac{g}{g_0} \left( \frac{\sigma_0}{\sigma} \right)^2 \quad (D6)$$

For all constituents of the atmosphere except oxygen in the region of dissociation,

$$\sigma = \sigma_0$$

In the absence of available data on the diameter of atoms of oxygen relative to that of molecular oxygen, and in consideration of the fact that the small difference in these two diameters of oxygen has an even smaller effect upon the average diameter of all atmospheric constituents, and for reasons of simplicity it is herein assumed for oxygen also that  $\sigma = \sigma_0$ . For the purpose of computing these tables therefore equation (D6) is simplified to

$$\frac{\lambda}{\lambda_0} = \frac{p_0}{p} \frac{T}{T_0} \frac{g}{g_0} \quad (D7)$$

Furthermore, in those computations that are based on a constant value for the acceleration of gravity

$$g = g_0$$

whence equation (D7) is further simplified to

$$\frac{\lambda}{\lambda_0} = \frac{p_0}{p} \frac{T}{T_0} \quad (D8)$$

#### Mean Free Paths of Molecules at Sea Level

The values of the mean free path of the molecules at sea level given in table I are for nitrogen and oxygen molecules in a normal atmospheric mixture of nitrogen and oxygen. These mean free paths are designated  $\lambda_n$  and  $\lambda_o$ , respectively. A weighted average of the foregoing mean free paths, based upon the relative volumes of nitrogen and oxygen in air is also included and is designated  $\lambda_{air}$ .

The mean free path of the nitrogen molecules in the atmosphere at sea level was computed by the following formula (p. 99 of reference 18):

$$\lambda_n = \frac{1}{\pi \sqrt{2} N_n \sigma_n^2 + \pi N_o \sigma^2 \frac{\sqrt{\bar{c}_n^2 + \bar{c}_o^2}}{\bar{c}_n}}$$



where

$N_n$  number of nitrogen molecules per unit volume of air

$N_o$  number of oxygen molecules per unit volume of air

$\sigma_n$  diameter of nitrogen molecules

$\sigma_o$  diameter of oxygen molecules

$\bar{\sigma}$  average diameter of nitrogen and oxygen molecules

$\bar{c}_n$  average speed of nitrogen molecules

$\bar{c}_o$  average speed of oxygen molecules

Similarly, the mean free path of the oxygen molecules at sea level was computed by

$$\lambda_o = \frac{1}{\pi \sqrt{2} N_o \sigma_o^2 + \pi N_n \bar{\sigma}^2 \frac{\sqrt{\bar{c}_n^2 + \bar{c}_o^2}}{\bar{c}_o}} \quad (D9)$$

The values for the average speeds  $\bar{c}_n$  and  $\bar{c}_o$  were obtained from

the formula  $\bar{c} = \sqrt{\frac{3RT}{M}}$ . The values for  $\sigma$  were taken from

appendix III, column 4, of reference 18. Values of  $N_n$  and  $N_o$ , the number of molecules of nitrogen and oxygen, respectively, per unit volume were calculated from the Loschmidt number and the relative volume of the nitrogen and oxygen in air at sea level.

## APPENDIX E

## VALUES OF CERTAIN CONSTANTS

## Tentative Standard Atmosphere at Sea Level

The standard sea-level values for various properties of the atmosphere have been listed in reference 1, and sea-level values for certain other properties are listed in reference 5. Most of these previously listed values are adopted for use in computing the tables herein, but a few changes have been made. The changes are as follows:

Speed of sound.- The values for the speed of sound have been altered slightly to avoid the discrepancy which existed between the values previously listed and the values computed by the conventional equation

$$a_0 = \sqrt{\frac{\gamma_0 p_0}{\rho_0}} \quad (E1)$$

The values for  $a_0$  listed in table I are computed according to equation (E1) by using the appropriate values for  $\gamma_0$ ,  $p_0$ , and  $\rho_0$  that are also listed in table I.

Density.- The values for density in the British engineering system has been changed from 0.002378 to 0.0023779 slugs per cubic foot to avoid discrepancies resulting when computations are based either on the standardized value for specific weight, 1.2255 kilograms per cubic meter (reference 1), or on the derived value for density.

Molecular mean free paths and molecular weight.- In addition to the various quantities previously given in references 1 and 5, the present paper lists molecular mean free paths and the average molecular weight of normal sea-level air. Molecular mean free paths for the nitrogen molecules and oxygen molecules in the normal air mixture have been computed and a weighted average for air has been taken, as described in appendix D. The average molecular weight of normal sea-level air is taken as 28.966 in accordance with reference 19.

Pressure.- The value for pressure in the British engineering system has been changed from 407.1 or 407.2 inches of water at 15° C as used in reference 5 and reference 20, respectively, to 407.15 inches of water at 15° C. This value of 407.15 is the computed value corresponding to 760 millimeters of mercury based on the auxiliary constants and conversion factors listed in the last section of this appendix E.

#### Table of Sea-Level Values

The values for the various properties of the atmosphere at sea level corresponding to the adopted values for probable minimum and probable maximum temperatures are computed from the values corresponding to standard sea-level temperatures. All three sets of values used in both metric and British engineering systems of units are tabulated in table I. In some instances a quantity is listed in more than one unit; in either the metric or British system.

#### Auxiliary Constants and Conversion Factors

In addition to the atmospheric properties at sea level given in table I certain other basic constants and conversion factors are used in computing tables II to V. They are

##### Auxiliary constants:

Density of mercury at 0° C, gm/cm <sup>3</sup> . . . . .	13.5951
Standard acceleration of gravity, g <sub>0</sub> , cm/sec <sup>2</sup> . . . . .	980.665
Density of water at 15° C, gm/ml . . . . .	0.9991286
Radius of the earth at 45° latitude and at sea level, m	6,367,623

##### Conversion factors:

$$\begin{aligned}
 1 \text{ lb} &= 453.5924 \text{ gm} \\
 1 \text{ meter} &= 3.280833 \text{ ft} \\
 ^\circ\text{K} &= ^\circ\text{C} + 273 \\
 ^\circ\text{F abs} &= ^\circ\text{F} + 459.4 \\
 1 \text{ ml} &= 1.000027 \text{ cm}^3
 \end{aligned}$$

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TABLE I.—PROPERTIES OF THE ATMOSPHERE AT SEA LEVEL

Quantity	Symbol	Metric engineering system				British engineering system			
		Unit	At probable minimum temperature	At standard temperature	At probable maximum temperature	Unit	At probable minimum temperature	At standard temperature	At probable maximum temperature
Temperature	$t_0$	$^{\circ}\text{C}$	-48.0	15.0	47.0	$^{\circ}\text{F}$	-54.5	59.0	116.6
Absolute temperature	$T_0$	$^{\circ}\text{K}$	225.0	288.0	320.0	$^{\circ}\text{F abs.}$	405.0	518.4	576.0
Pressure	$p_0$	mm Hg at $0^{\circ}\text{C}$	760	760	760	in. Hg at $32^{\circ}\text{F}$	29.9212	29.9212	29.9212
		$\text{kg}/\text{m}^2$	10332.3	10332.3	10332.3	in. water at $15^{\circ}\text{C}$	407.15	407.15	407.15
		$\text{dynes}/\text{cm}^2$	$1.01325 \times 10^6$	$1.01325 \times 10^6$	$1.01325 \times 10^6$	$\text{lb}/\text{ft}^2$	2116.23	2116.23	2116.23
Specific weight	$\gamma_0$	$\text{kg}/\text{m}^3$	1.5686	1.2255	1.1030	$\text{lb}/\text{ft}^3$	0.097928	0.076506	0.068855
Density	$\rho_0 = \frac{\gamma_0}{g_0}$	$\text{dynes}/\text{cm}^3$	1.5383	1.2018	1.0816	$\text{slugs}/\text{ft}^3$	0.0030437	0.0023779	0.0021401
		$\text{kg-sec}/\text{m}^4$	0.15995	0.124966	0.11247				
Coefficient of viscosity	$\mu_0$	$\text{kg-sec}/\text{m}^2$	$1.4852 \times 10^{-6}$	$1.8187 \times 10^{-6}$	$1.9751 \times 10^{-6}$	$\text{lb-sec}/\text{ft}^2$	$3.0420 \times 10^{-7}$	$3.7250 \times 10^{-7}$	$4.0455 \times 10^{-7}$
		poise ( $\text{dynes-sec}/\text{cm}^2$ )	$1.4565 \times 10^{-8}$	$1.7835 \times 10^{-8}$	$1.9369 \times 10^{-8}$				
Kinematic viscosity	$\nu_0 = \frac{\mu_0}{\rho_0}$	$\text{m}^2/\text{sec}$	$9.2848 \times 10^{-6}$	$14.553 \times 10^{-6}$	$17.561 \times 10^{-6}$	$\text{ft}^2/\text{sec}$	$0.9994 \times 10^{-4}$	$1.5665 \times 10^{-4}$	$1.8903 \times 10^{-4}$
Speed of sound	$a_0$	$\text{m}/\text{sec}$	300.72	340.22	358.63	$\text{ft}/\text{sec}$	986.61	1116.22	1176.60
		$\text{km}/\text{hr}$	1082.6	1224.8	1291.1	$\text{mph}$	672.69	761.06	802.23
						knots	584.16	660.90	696.65
Mean free path of nitrogen molecules	$\lambda_n$	m	$5.76 \times 10^{-8}$	$7.38 \times 10^{-8}$	$8.20 \times 10^{-8}$	ft	$0.1891 \times 10^{-6}$	$0.2421 \times 10^{-6}$	$0.2690 \times 10^{-6}$
Mean free path of oxygen molecules	$\lambda_o$	m	$5.75 \times 10^{-8}$	$7.36 \times 10^{-8}$	$8.18 \times 10^{-8}$	ft	$0.1887 \times 10^{-6}$	$0.2415 \times 10^{-6}$	$0.2683 \times 10^{-6}$
Mean free path of air molecules	$\lambda_{air}$	m	$5.76 \times 10^{-8}$	$7.37 \times 10^{-8}$	$8.19 \times 10^{-8}$	ft	$0.1890 \times 10^{-6}$	$0.2419 \times 10^{-6}$	$0.2688 \times 10^{-6}$
Average molecular weight	$M_0$	----	28.966	28.966	28.966	----	28.966	28.966	28.966
Ratio of specific heats	$\gamma_0$	----	1.4	1.4	1.4	----	1.4	1.4	1.4
Relative volume of oxygen	$x_0$	----	0.2095	0.2095	0.2095	----	0.2095	0.2095	0.2095

## TABLES II AND III

PROPERTIES OF THE UPPER ATMOSPHERE  
FOR TENTATIVE STANDARD TEMPERATURES  
BASED ON AN ARBITRARY CONSTANT VALUE  
OF GRAVITATIONAL FORCE

The following set of two tables (tables II and III) constitutes a consistent extension of the standard tables for the lower atmosphere (NACA Rep. No. 218). Consequently, altitudes in this set of tables which correspond to specified ambient-air pressures may be referred to as "tentative pressure altitudes," and those which correspond to a specified ambient-air density may be referred to as "tentative density altitudes" (NACA Rep. No. 474).

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TABLE II.—PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN ARBITRARY  
CONSTANT VALUE OF GRAVITATIONAL FORCE — METRIC ENGINEERING SYSTEM

Altitude, h (m)	Absolute temperature, T (°K)	Pressure, P (kg/m <sup>2</sup> )	Pressure ratio, P/P <sub>0</sub>	Density, $\rho$ (kg-m <sup>3</sup> )	Density ratio, $\rho/\rho_0$	Specific weight, $\gamma$ (kg/m <sup>3</sup> )	Coefficient of viscosity, $\mu$ (kg-sec/m <sup>2</sup> )	Kinematic viscosity, $\nu = \mu/\rho$ (m <sup>2</sup> /sec)	Speed of sound, a (m/sec)	Mean free path of molecules, $\lambda$ (m)
(a) For both day and night										
20,000	218.0	563.0	5440-10 <sup>-5</sup>	899-10 <sup>-6</sup>	7198-10 <sup>-5</sup>	8821-10 <sup>-5</sup>	1.446-10 <sup>-6</sup>	0.01607-10 <sup>-2</sup>	296.0	0.00102-10 <sup>-3</sup>
20,500	218.0	520.5	5038	8318	6656	8177	1.446	0.01738	296.0	0.00111
21,000	218.0	481.3	4658	7690	6184	7542	1.446	0.01880	296.0	0.00120
21,500	218.0	445.0	4307	7110	5690	6973	1.446	0.02033	296.0	0.00130
22,000	218.0	411.5	3983	6573	5251	6448	1.446	0.02199	296.0	0.00140
22,500	218.0	380.5	3683	6060	4824	5922	1.446	0.02378	296.0	0.00151
23,000	218.0	351.6	3405	5622	4426	5513	1.446	0.02572	296.0	0.00164
23,500	218.0	325.3	3148	5198	4059	5097	1.446	0.02782	296.0	0.00177
24,000	218.0	300.8	2911	4805	3744	4713	1.446	0.03008	296.0	0.00192
24,500	218.0	278.1	2692	4444	3458	4358	1.446	0.03254	296.0	0.00207
25,000	218.0	257.9	2489	4109	3208	4030	1.446	0.03518	296.0	0.00224
25,500	218.0	239.8	2301	3800	2980	3726	1.446	0.03800	296.0	0.00242
26,000	218.0	223.9	2128	3513	2781	3445	1.446	0.04115	296.0	0.00262
26,500	218.0	209.3	1968	3248	2599	3186	1.446	0.04461	296.0	0.00284
27,000	218.0	196.0	1820	3004	2440	2946	1.446	0.04831	296.0	0.00307
27,500	218.0	183.8	1682	2777	2292	2724	1.446	0.05230	296.0	0.00332
28,000	218.0	172.7	1555	2568	2158	2518	1.446	0.05659	296.0	0.00358
28,500	218.0	162.6	1438	2375	1990	2329	1.446	0.06089	296.0	0.00388
29,000	218.0	153.4	1330	2196	1787	2153	1.446	0.06568	296.0	0.00419
29,500	218.0	145.1	1230	2030	1655	1991	1.446	0.07122	296.0	0.00454
30,000	218.0	137.7	1137	1878	1503	1841	1.446	0.07700	296.0	0.00490
30,500	218.0	130.4	1051	1736	1381	1702	1.446	0.08330	296.0	0.00528
31,000	218.0	124.1	972.1	1604	1264	1574	1.446	0.09009	296.0	0.00567
31,500	218.0	117.8	898.9	1484	1157	1455	1.446	0.09743	296.0	0.00608
32,000	218.0	112.5	831.1	1372	1058	1346	1.446	0.10524	296.0	0.00651
32,500	218.0	107.2	769.0	1269	969.1	1244	1.446	0.11355	296.0	0.00697
33,000	218.0	102.0	711.8	1173	887.4	1146	1.446	0.12237	296.0	0.00745
33,500	218.0	96.8	658.8	1089	811.0	1058	1.446	0.13172	296.0	0.00795
34,000	218.0	91.6	610.7	1013	740.3	980.9	1.446	0.14160	296.0	0.00847
34,500	218.0	86.5	567.6	943.9	675.3	904.2	1.446	0.15202	296.0	0.00901
35,000	218.0	81.5	529.1	882.1	624.7	838.0	1.446	0.16300	296.0	0.00957
35,500	218.0	76.6	494.0	827.0	577.9	781.0	1.446	0.17454	296.0	0.01016
36,000	218.0	71.8	462.8	777.7	535.4	732.9	1.446	0.18665	296.0	0.01078
36,500	218.0	67.1	435.0	732.9	497.4	686.1	1.446	0.19934	296.0	0.01142
37,000	218.0	62.5	409.9	692.4	463.4	641.5	1.446	0.21262	296.0	0.01209
37,500	218.0	58.0	387.9	656.1	433.0	600.0	1.446	0.22650	296.0	0.01279
38,000	218.0	53.6	368.0	623.1	405.9	561.5	1.446	0.24098	296.0	0.01351
38,500	218.0	49.3	349.8	592.0	381.5	526.0	1.446	0.25606	296.0	0.01426
39,000	218.0	45.1	333.0	562.8	359.6	493.5	1.446	0.27174	296.0	0.01503
39,500	218.0	41.0	317.4	534.2	339.9	463.8	1.446	0.28802	296.0	0.01582
40,000	218.0	37.0	297.4	507.1	320.7	436.4	1.446	0.30490	296.0	0.01663
40,500	218.0	33.1	283.2	481.2	299.1	412.4	1.446	0.32238	296.0	0.01746
41,000	218.0	29.3	269.7	456.4	278.6	390.3	1.446	0.34046	296.0	0.01831
41,500	218.0	25.6	257.8	433.6	259.4	369.9	1.446	0.35914	296.0	0.01918
42,000	218.0	22.1	246.5	412.5	241.9	351.0	1.446	0.37842	296.0	0.02007
42,500	218.0	18.7	235.6	393.0	226.0	333.6	1.446	0.39830	296.0	0.02098
43,000	218.0	15.5	225.1	375.0	211.3	317.7	1.446	0.41878	296.0	0.02191
43,500	218.0	12.4	215.0	358.4	198.0	303.4	1.446	0.43986	296.0	0.02286
44,000	218.0	9.4	205.3	343.2	186.0	290.4	1.446	0.46154	296.0	0.02383
44,500	218.0	6.5	196.0	329.3	175.2	278.6	1.446	0.48382	296.0	0.02482
45,000	218.0	3.7	187.1	316.7	165.6	268.0	1.446	0.50670	296.0	0.02583
45,500	218.0	1.0	178.7	305.3	157.2	258.4	1.446	0.53018	296.0	0.02686
46,000	218.0	0.3	170.8	295.0	149.9	249.7	1.446	0.55426	296.0	0.02791
46,500	218.0	0.1	163.4	285.7	143.6	242.1	1.446	0.57894	296.0	0.02898
47,000	218.0	0.0	156.5	277.2	138.2	235.6	1.446	0.60422	296.0	0.03007
47,500	218.0	0.0	150.0	269.6	133.7	230.1	1.446	0.63010	296.0	0.03118
48,000	218.0	0.0	144.0	262.8	129.9	225.6	1.446	0.65658	296.0	0.03231
48,500	218.0	0.0	138.3	256.8	126.6	222.2	1.446	0.68366	296.0	0.03346
49,000	218.0	0.0	133.0	251.3	123.7	219.7	1.446	0.71134	296.0	0.03463
49,500	218.0	0.0	128.0	246.3	121.1	217.1	1.446	0.73962	296.0	0.03581
50,000	218.0	0.0	123.2	241.7	118.8	215.4	1.446	0.76850	296.0	0.03701
50,500	218.0	0.0	118.6	237.4	116.7	213.7	1.446	0.79798	296.0	0.03822
51,000	218.0	0.0	114.2	233.4	114.8	212.0	1.446	0.82806	296.0	0.03945
51,500	218.0	0.0	110.0	229.6	113.0	210.3	1.446	0.85874	296.0	0.04069
52,000	218.0	0.0	106.0	226.0	111.3	208.6	1.446	0.88992	296.0	0.04195
52,500	218.0	0.0	102.1	222.6	109.7	207.0	1.446	0.92160	296.0	0.04322
53,000	218.0	0.0	98.2	219.3	108.2	205.4	1.446	0.95388	296.0	0.04450
53,500	218.0	0.0	94.4	216.1	106.7	203.8	1.446	0.98676	296.0	0.04579
54,000	218.0	0.0	90.7	213.0	105.2	202.2	1.446	1.02014	296.0	0.04709
54,500	218.0	0.0	87.1	210.0	103.7	200.6	1.446	1.05402	296.0	0.04840
55,000	218.0	0.0	83.6	207.1	102.2	199.0	1.446	1.08840	296.0	0.04972
55,500	218.0	0.0	80.1	204.2	100.7	197.4	1.446	1.12328	296.0	0.05105
56,000	218.0	0.0	76.7	201.3	99.2	195.8	1.446	1.15866	296.0	0.05239
56,500	218.0	0.0	73.3	198.4	97.7	194.2	1.446	1.19454	296.0	0.05374
57,000	218.0	0.0	70.0	195.5	96.2	192.6	1.446	1.23092	296.0	0.05510
57,500	218.0	0.0	66.7	192.6	94.7	191.0	1.446	1.26780	296.0	0.05646
58,000	218.0	0.0	63.5	189.7	93.2	189.4	1.446	1.30518	296.0	0.05783
58,500	218.0	0.0	60.3	186.8	91.7	187.8	1.446	1.34306	296.0	0.05920
59,000	218.0	0.0	57.2	183.9	90.2	186.2	1.446	1.38144	296.0	0.06058
59,500	218.0	0.0	54.1	181.0	88.7	184.6	1.446	1.42032	296.0	0.06196
60,000	218.0	0.0	51.1	178.1	87.2	183.0	1.446	1.45970	296.0	0.06335
60,500	218.0	0.0	48.1	175.2	85.7	181.4	1.446	1.50000	296.0	0.06474
61,000	218.0	0.0	45.2	172.3	84.2	179.8	1.446	1.54120	296.0	0.06614
61,500	218.0	0.0	42.3	169.4	82.7	178.2	1.446	1.58340	296.0	0.06754
62,000	218.0	0.0	39.4	166.5	81.2	176.6	1.446	1.62660	296.0	0.06895
62,500	218.0	0.0	36.5	163.6	79.7	175.0	1.446	1.67080	296.0	0.07036
63,000	218.0	0.0	33.6	160.7	78.2	173.4	1.446	1.71600	296.0	0.07177
63,500	218.0	0.0	30.7	157.8	76.7	171.8	1.446	1.76220	296.0	0.07318
64,000	218.0	0.0	27.8	154.9	75.2	170.2	1.446	1.80940	296.0	0.07460
64,500	218.0	0.0	24.9	152.0	73.7	168.6	1.446	1.85760	296.0	0.07602
65,000	218.0	0.0	22.0	149.1	72.2	167.0	1.446	1.90680	296.0	0.07744
65,500	218.0	0.0	19.1	146.2	70.7	165.4	1.446	1.95700	296.0	0.07886
66,000	218.0	0.0	16.2	143.3	69.2	163.8	1.446	2.00820	296.0	0.08028
66,500	218.0	0.0	13.3	140.4	67.7	162.2	1.446	2.06040	296.0	0.08170
67,000	218.0	0.0	10.4	137.5	66.2	160.6	1.446	2.11360	296.0	0.08312
67,500	218.0	0.0	7.5	134.6	64.7	159.0	1.446	2.16780	296.0	0.08454
68,000	218.0	0.0	4.6	131.7	63.2	157.4	1.446	2.22300	296.0	0.08596
68,500	218.0	0.0	1.7	128.8	61.7	155.8	1.446	2.27920	296.0	0.08738
69,000	218.0	0.0	0.0	125.9	60.2	154.2	1.446	2.33640	296.0	0.08880
69,500	218.0	0.0	0.0	123.0	58.7	152.6	1.446	2.39460	296.0	0.09022
70,000	218.0	0.0	0.0	120.1	57.2	151				



TABLE II.—PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN ARBITRARY  
CONSTANT VALUE OF GRAVITATIONAL FORCE — METRIC ENGINEERING SYSTEM — Concluded

Altitude, h (m)	Absolute tempera- ture, T (°K)	Pressure, P (kg/m <sup>2</sup> )	Pressure ratio, P/P <sub>0</sub>	Density, ρ (kg-sec <sup>2</sup> /m <sup>4</sup> )	Density ratio, σ = ρ/ρ <sub>0</sub>	Specific weight, γ = gρ (kg/m <sup>3</sup> )	Coefficient of viscosity, μ (kg-sec/m <sup>2</sup> ) (1)	Kinematic viscosity, ν = μ/ρ (m <sup>2</sup> /sec) (1)	Speed of sound, a (m/sec)	Mean free path of molecules, λ (m)
(b) For day only										
80,000	240.0	0.3256	3151×10 <sup>-8</sup>	4726×10 <sup>-9</sup>	3782×10 <sup>-8</sup>	4635×10 <sup>-8</sup>	1.568×10 <sup>-6</sup>	0.3318	310.6	1.99×10 <sup>-3</sup>
81,000	240.0	0.2824	2733	4060	3248	3981	1.568	0.3825	310.6	2.25
82,000	240.0	0.2450	2371	3555	2845	3486	1.568	0.4411	310.6	2.59
83,000	240.0	0.2129	2070	3009	2408	2951	1.568	0.5085	310.6	2.99
84,000	243.6	0.1856	1806	2561	2049	2512	1.568	0.6200	320.8	3.45
85,000	247.3	0.1634	1582	2188	1751	2145	1.607	0.7348	325.2	4.00
86,000	250.9	0.1435	1389	1874	1500	1838	1.627	0.8682	329.6	4.62
87,000	254.6	0.1265	1224	1612	1290	1581	1.646	1.021	333.9	5.32
88,000	258.2	0.1118	1082	1391	1113	1364	1.666	1.197	338.3	6.11
89,000	261.9	0.09908	959.0	1204	963.7	1181	1.685	1.400	342.7	6.99
90,000	265.5	0.08810	852.7	1046	837.1	1026	1.704	1.629	347.1	7.97
91,000	269.2	0.07850	759.7	910.9	728.9	893.2	1.723	1.892	351.5	9.07
92,000	272.8	0.07016	679.0	795.7	636.7	780.3	1.742	2.189	355.9	10.3
93,000	276.5	0.06285	608.3	697.0	557.8	683.5	1.760	2.526	360.4	11.6
94,000	280.1	0.05643	546.1	611.3	489.7	604.1	1.779	2.907	364.8	13.1
95,000	283.8	0.05079	491.6	538.8	431.1	525.4	1.797	3.326	369.2	14.8
96,000	287.4	0.04584	443.7	475.8	380.7	466.6	1.816	3.781	373.7	16.6
97,000	291.1	0.04144	401.1	421.0	336.9	412.9	1.834	4.267	378.1	18.6
98,000	294.7	0.03756	363.5	373.5	298.9	366.3	1.852	4.790	382.6	20.7
99,000	298.4	0.03410	330.1	332.0	265.7	325.6	1.870	5.333	387.1	23.1
100,000	302.0	0.03102	300.2	295.8	236.7	290.1	1.888	6.393	391.5	25.7
101,000	305.7	0.02827	273.6	263.3	213.1	263.2	1.906	7.579	395.9	28.6
102,000	309.3	0.02579	249.6	240.1	192.1	235.5	1.924	8.911	400.3	31.7
103,000	313.0	0.02355	227.9	217.4	173.4	212.5	1.941	10.399	404.6	35.1
104,000	316.6	0.02153	208.4	195.8	156.7	192.0	1.959	12.00	408.9	38.9
105,000	320.3	0.01970	190.7	177.2	141.6	173.7	1.976	13.74	413.2	43.0
106,000	323.9	0.01805	174.7	160.5	128.4	157.4	1.994	15.62	417.5	47.5
107,000	327.6	0.01655	160.2	145.5	116.4	142.7	2.011	17.64	421.7	52.3
108,000	331.2	0.01519	147.0	132.1	105.7	129.5	2.028	19.86	425.9	57.7
109,000	334.9	0.01395	135.1	120.0	96.03	117.7	2.045	22.34	430.1	63.5
110,000	338.5	0.01283	124.2	109.2	87.35	107.1	2.060	25.09	434.5	69.8
111,000	342.2	0.01181	114.3	99.40	79.54	97.48	2.079	28.02	438.7	76.8
112,000	345.8	0.01088	105.3	90.60	72.50	88.85	2.096	31.13	442.9	84.0
113,000	349.5	0.01003	97.08	82.66	66.14	81.06	2.113	34.46	447.1	91.1
114,000	353.1	0.00925	89.58	75.49	60.40	74.02	2.129	38.02	451.3	98.1
115,000	356.8	0.00854	82.78	69.00	55.21	67.66	2.146	41.80	455.5	105.0
116,000	360.4	0.007900	76.42	63.13	51.01	61.91	2.162	45.82	459.7	121
117,000	364.1	0.007308	70.73	57.81	46.26	56.69	2.179	50.09	463.9	132
118,000	367.7	0.006765	65.47	52.98	42.40	51.96	2.195	54.62	468.0	144
119,000	371.4	0.006267	60.66	48.60	38.89	47.66	2.211	59.40	472.1	157
120,000	375.0	0.005810	56.24	44.62	35.71	43.76	2.227	64.43	476.3	171
(c) For night only										
80,000	240.0	0.3256	3151×10 <sup>-8</sup>	4726×10 <sup>-9</sup>	3782×10 <sup>-8</sup>	4635×10 <sup>-8</sup>	1.568×10 <sup>-6</sup>	0.3318	310.6	1.99×10 <sup>-3</sup>
81,000	240.0	0.2824	2733	4099	3280	4020	1.568	0.3825	310.6	2.25
82,000	240.0	0.2450	2371	3555	2845	3486	1.568	0.4411	310.6	2.59
83,000	240.0	0.2129	2070	3008	2467	3024	1.568	0.5085	310.6	2.99
84,000	243.6	0.1845	1785	2637	2110	2586	1.568	0.6021	312.9	3.49
85,000	247.3	0.1605	1553	2261	1807	2217	1.607	0.7110	315.3	4.07
86,000	250.9	0.1399	1354	1943	1554	1905	1.627	0.8376	317.7	4.74
87,000	254.6	0.1222	1183	1673	1338	1640	1.645	0.9834	319.9	5.51
88,000	258.2	0.1070	1036	1443	1155	1415	1.666	1.154	322.2	6.38
89,000	261.9	0.09383	908.1	1248	1008	1224	1.685	1.350	324.4	7.38
90,000	265.5	0.08243	797.8	1081	865.3	1060	1.704	1.576	326.7	8.52
91,000	269.2	0.07254	702.1	938.8	751.2	920.6	1.723	1.835	328.9	9.81
92,000	272.8	0.06395	618.9	816.5	653.3	800.6	1.742	2.133	331.1	11.3
93,000	276.5	0.05647	546.6	711.5	569.3	697.7	1.760	2.474	333.4	12.9
94,000	280.1	0.04995	483.4	621.1	497.0	609.1	1.779	2.864	335.5	14.8
95,000	283.8	0.04425	428.3	543.2	434.6	532.7	1.798	3.309	337.7	17.0
96,000	287.4	0.03926	380.0	475.8	380.7	466.6	1.816	3.816	339.9	19.4
97,000	291.1	0.03489	337.7	417.5	334.1	409.4	1.834	4.393	342.0	22.1
98,000	294.7	0.03105	300.5	367.0	293.6	352.8	1.852	5.048	344.2	25.1
99,000	298.4	0.02767	267.8	323.0	259.5	316.8	1.870	5.790	346.3	28.5
100,000	302.0	0.02469	239.0	284.8	227.9	279.3	1.888	6.630	348.4	32.3
101,000	305.7	0.02207	213.6	251.5	201.2	246.6	1.906	7.579	350.5	36.6
102,000	309.3	0.01975	191.1	222.4	178.0	218.1	1.924	8.651	352.6	41.4
103,000	313.0	0.01770	171.3	197.0	157.6	193.1	1.942	9.869	354.7	46.8
104,000	316.6	0.01588	153.6	174.7	139.8	171.3	1.959	11.22	356.7	52.7
105,000	320.3	0.01426	138.0	158.1	124.1	152.1	1.976	12.74	358.8	59.4
106,000	323.9	0.01284	124.2	136.2	109.0	133.5	1.994	14.44	360.9	66.7
107,000	327.6	0.01158	112.1	119.8	95.89	117.5	2.011	16.38	363.0	74.8
108,000	331.2	0.01048	101.4	105.8	84.62	103.7	2.028	18.48	374.1	83.6
109,000	334.9	0.009501	91.95	93.60	74.90	91.79	2.045	21.85	379.2	93.2
110,000	338.5	0.008636	83.58	83.06	66.47	81.46	2.062	24.83	384.3	104
111,000	342.2	0.007867	76.14	73.90	59.13	72.47	2.079	28.14	389.4	115
112,000	345.8	0.007183	69.52	65.91	52.74	64.63	2.096	31.80	394.6	127
113,000	349.5	0.006573	63.62	58.93	47.16	57.79	2.113	35.85	399.8	141
114,000	353.1	0.006026	58.32	52.80	42.25	51.78	2.129	40.33	404.9	155
115,000	356.8	0.005534	53.56	47.41	37.94	46.49	2.146	45.26	410.1	170
116,000	360.4	0.005091	49.28	42.66	34.13	41.83	2.162	50.69	415.3	187
117,000	364.1	0.004692	45.44	38.47	30.76	37.73	2.179	56.53	420.6	205
118,000	367.7	0.004335	41.97	34.77	27.62	34.09	2.196	62.84	426.0	224
119,000	371.4	0.004011	38.82	31.47	24.88	30.82	2.211	70.27	431.0	245
120,000	375.0	0.003718	35.93	28.55	22.85	28.00	2.227	78.01	436.3	267

<sup>1</sup>The values for viscosity listed in these columns are not applicable at the higher altitudes where the mean free path of the molecules are comparable to or longer than the dimensions of the body being considered. Furthermore, the values listed are based on the conventional Sutherland formula for normal air and, consequently, no allowance has been made for the effect of dissociated oxygen in the atmosphere at the higher levels.

TABLE III. - PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN ARBITRARY CONSTANT VALUE OF GRAVITATIONAL FORCE - BRITISH ENGINEERING SYSTEM

Altitude, (ft)	Absolute temperature, ° (°F abs.)	Pressure, (lb./in. <sup>2</sup> )	Pressure ratio, P/P <sub>0</sub>	Density, ρ (slugs/ft. <sup>3</sup> )	Density ratio, σ = ρ/ρ <sub>0</sub>	Specific weight, γ = γ <sub>0</sub> (lb./ft. <sup>3</sup> )	Coefficient of viscosity, μ = μ <sub>0</sub> (lb.-sec./ft. <sup>2</sup> )	Kinematic viscosity, ν = ν <sub>0</sub> (ft. <sup>2</sup> /sec.)	Speed of sound, a (ft./sec.)	Mean free path of molecules, λ (ft.)
(a) For both day and night										
69,000	392.4	118.8	5612x10 <sup>-5</sup>	1.78x10 <sup>-7</sup>	7.41x10 <sup>-5</sup>	5672x10 <sup>-6</sup>	2.96x10 <sup>-4</sup>	0.001690	971.1	0.00326x10 <sup>-3</sup>
68,000	392.4	113.2	5390	1.76	7.36	5652	2.961	0.001691	971.1	0.00326
67,000	392.4	107.6	5168	1.74	7.31	5632	2.961	0.001692	971.1	0.00326
66,000	392.4	102.0	4946	1.72	7.26	5612	2.961	0.001693	971.1	0.00326
65,000	392.4	96.4	4724	1.70	7.21	5592	2.961	0.001694	971.1	0.00326
70,000	392.4	93.52	4419	1.68	7.16	5572	2.961	0.001695	971.1	0.00326
71,000	392.4	89.16	4243	1.66	7.11	5552	2.961	0.001696	971.1	0.00326
72,000	392.4	84.80	4067	1.64	7.06	5532	2.961	0.001697	971.1	0.00326
73,000	392.4	80.44	3891	1.62	7.01	5512	2.961	0.001698	971.1	0.00326
74,000	392.4	76.08	3715	1.60	6.96	5492	2.961	0.001699	971.1	0.00326
75,000	392.4	71.72	3539	1.58	6.91	5472	2.961	0.001700	971.1	0.00326
76,000	392.4	67.36	3363	1.56	6.86	5452	2.961	0.001701	971.1	0.00326
77,000	392.4	63.00	3187	1.54	6.81	5432	2.961	0.001702	971.1	0.00326
78,000	392.4	58.64	3011	1.52	6.76	5412	2.961	0.001703	971.1	0.00326
79,000	392.4	54.28	2835	1.50	6.71	5392	2.961	0.001704	971.1	0.00326
80,000	392.4	50.00	2659	1.48	6.66	5372	2.961	0.001705	971.1	0.00326
81,000	392.4	45.64	2483	1.46	6.61	5352	2.961	0.001706	971.1	0.00326
82,000	392.4	41.28	2307	1.44	6.56	5332	2.961	0.001707	971.1	0.00326
83,000	392.4	36.92	2131	1.42	6.51	5312	2.961	0.001708	971.1	0.00326
84,000	392.4	32.56	1955	1.40	6.46	5292	2.961	0.001709	971.1	0.00326
85,000	392.4	28.20	1779	1.38	6.41	5272	2.961	0.001710	971.1	0.00326
86,000	392.4	23.84	1603	1.36	6.36	5252	2.961	0.001711	971.1	0.00326
87,000	392.4	19.48	1427	1.34	6.31	5232	2.961	0.001712	971.1	0.00326
88,000	392.4	15.12	1251	1.32	6.26	5212	2.961	0.001713	971.1	0.00326
89,000	392.4	10.76	1075	1.30	6.21	5192	2.961	0.001714	971.1	0.00326
90,000	392.4	6.40	900	1.28	6.16	5172	2.961	0.001715	971.1	0.00326
91,000	392.4	2.04	724	1.26	6.11	5152	2.961	0.001716	971.1	0.00326
92,000	392.4	1.68	600	1.24	6.06	5132	2.961	0.001717	971.1	0.00326
93,000	392.4	1.32	476	1.22	6.01	5112	2.961	0.001718	971.1	0.00326
94,000	392.4	0.96	352	1.20	5.96	5092	2.961	0.001719	971.1	0.00326
95,000	392.4	0.60	228	1.18	5.91	5072	2.961	0.001720	971.1	0.00326
96,000	392.4	0.24	104	1.16	5.86	5052	2.961	0.001721	971.1	0.00326
97,000	392.4	0.08	40	1.14	5.81	5032	2.961	0.001722	971.1	0.00326
98,000	392.4	0.03	15	1.12	5.76	5012	2.961	0.001723	971.1	0.00326
99,000	392.4	0.01	5	1.10	5.71	5000	2.961	0.001724	971.1	0.00326
100,000	392.4	0.00	0	1.08	5.66	4988	2.961	0.001725	971.1	0.00326
101,000	392.4	0.00	0	1.06	5.61	4968	2.961	0.001726	971.1	0.00326
102,000	392.4	0.00	0	1.04	5.56	4948	2.961	0.001727	971.1	0.00326
103,000	392.4	0.00	0	1.02	5.51	4928	2.961	0.001728	971.1	0.00326
104,000	392.4	0.00	0	1.00	5.46	4908	2.961	0.001729	971.1	0.00326
105,000	392.4	0.00	0	0.98	5.41	4888	2.961	0.001730	971.1	0.00326
106,000	392.4	0.00	0	0.96	5.36	4868	2.961	0.001731	971.1	0.00326
107,000	392.4	0.00	0	0.94	5.31	4848	2.961	0.001732	971.1	0.00326
108,000	392.4	0.00	0	0.92	5.26	4828	2.961	0.001733	971.1	0.00326
109,000	392.4	0.00	0	0.90	5.21	4808	2.961	0.001734	971.1	0.00326
110,000	392.4	0.00	0	0.88	5.16	4788	2.961	0.001735	971.1	0.00326
111,000	392.4	0.00	0	0.86	5.11	4768	2.961	0.001736	971.1	0.00326
112,000	392.4	0.00	0	0.84	5.06	4748	2.961	0.001737	971.1	0.00326
113,000	392.4	0.00	0	0.82	5.01	4728	2.961	0.001738	971.1	0.00326
114,000	392.4	0.00	0	0.80	4.96	4708	2.961	0.001739	971.1	0.00326
115,000	392.4	0.00	0	0.78	4.91	4688	2.961	0.001740	971.1	0.00326
116,000	392.4	0.00	0	0.76	4.86	4668	2.961	0.001741	971.1	0.00326
117,000	392.4	0.00	0	0.74	4.81	4648	2.961	0.001742	971.1	0.00326
118,000	392.4	0.00	0	0.72	4.76	4628	2.961	0.001743	971.1	0.00326
119,000	392.4	0.00	0	0.70	4.71	4608	2.961	0.001744	971.1	0.00326
120,000	392.4	0.00	0	0.68	4.66	4588	2.961	0.001745	971.1	0.00326
121,000	392.4	0.00	0	0.66	4.61	4568	2.961	0.001746	971.1	0.00326
122,000	392.4	0.00	0	0.64	4.56	4548	2.961	0.001747	971.1	0.00326
123,000	392.4	0.00	0	0.62	4.51	4528	2.961	0.001748	971.1	0.00326
124,000	392.4	0.00	0	0.60	4.46	4508	2.961	0.001749	971.1	0.00326
125,000	392.4	0.00	0	0.58	4.41	4488	2.961	0.001750	971.1	0.00326
126,000	392.4	0.00	0	0.56	4.36	4468	2.961	0.001751	971.1	0.00326
127,000	392.4	0.00	0	0.54	4.31	4448	2.961	0.001752	971.1	0.00326
128,000	392.4	0.00	0	0.52	4.26	4428	2.961	0.001753	971.1	0.00326
129,000	392.4	0.00	0	0.50	4.21	4408	2.961	0.001754	971.1	0.00326
130,000	392.4	0.00	0	0.48	4.16	4388	2.961	0.001755	971.1	0.00326
131,000	392.4	0.00	0	0.46	4.11	4368	2.961	0.001756	971.1	0.00326
132,000	392.4	0.00	0	0.44	4.06	4348	2.961	0.001757	971.1	0.00326
133,000	392.4	0.00	0	0.42	4.01	4328	2.961	0.001758	971.1	0.00326
134,000	392.4	0.00	0	0.40	3.96	4308	2.961	0.001759	971.1	0.00326
135,000	392.4	0.00	0	0.38	3.91	4288	2.961	0.001760	971.1	0.00326
136,000	392.4	0.00	0	0.36	3.86	4268	2.961	0.001761	971.1	0.00326
137,000	392.4	0.00	0	0.34	3.81	4248	2.961	0.001762	971.1	0.00326
138,000	392.4	0.00	0	0.32	3.76	4228	2.961	0.001763	971.1	0.00326
139,000	392.4	0.00	0	0.30	3.71	4208	2.961	0.001764	971.1	0.00326
140,000	392.4	0.00	0	0.28	3.66	4188	2.961	0.001765	971.1	0.00326
141,000	392.4	0.00	0	0.26	3.61	4168	2.961	0.001766	971.1	0.00326
142,000	392.4	0.00	0	0.24	3.56	4148	2.961	0.001767	971.1	0.00326
143,000	392.4	0.00	0	0.22	3.51	4128	2.961	0.001768	971.1	0.00326
144,000	392.4	0.00	0	0.20	3.46	4108	2.961	0.001769	971.1	0.00326
145,000	392.4	0.00	0	0.18	3.41	4088	2.961	0.001770	971.1	0.00326
146,000	392.4	0.00	0	0.16	3.36	4068	2.961	0.001771	971.1	0.00326
147,000	392.4	0.00	0	0.14	3.31	4048	2.961	0.001772	971.1	0.00326
148,000	392.4	0.00	0	0.12	3.26	4028	2.961	0.001773	971.1	0.00326
149,000	392.4	0.00	0	0.10	3.21	4008	2.961	0.001774	971.1	0.00326
150,000	392.4	0.00	0	0.08	3.16	3988	2.961	0.001775	971.1	0.00326
151,000	392.4	0.00	0	0.06	3.11	3968	2.961	0.001776	971.1	0.00326
152,000	392.4	0.00	0	0.04	3.06	3948	2.961	0.001777	971.1	0.00326
153,000	392.4	0.00	0	0.02	3.01	3928	2.961	0.001778	971.1	0.00326
154,000	392.4	0.00	0	0.00	2.96	3908	2.961	0.001779	971.1	0.00326
155,000	392.4	0.00	0	0.00	2.91	3888	2.961	0.001780	971.1	0.00326
156,000	392.4	0.00	0	0.00	2.86	3868	2.961	0.001781	971.1	0.00326
157,000	392.4	0.00	0	0.00	2.81	3848	2.961	0.001782	971.1	0.00326
158,000	392.4	0.00	0	0.00	2.76	3828	2.961	0.001783	971.1	0.00326
159,000	392.4	0.00	0	0.00	2.71	3808	2.961	0.001784	971.1	0.00326
160,000	392.4	0.00	0	0.00	2.66	3788	2.961	0.001785	971.1	0.00326
161,000	392.4	0.00	0	0.00	2.61	3768	2.961	0.001786	971.1	0.00326
162,000	392.4	0.00	0	0.00	2.56	3748	2.961	0.001787	971.1	0.00326
163,000	392.4	0.00	0	0.00	2.51	3728	2.961	0.001788	971.1	0.00326
164,000	392.4	0.00	0	0.00	2.46	3708	2.961	0.001789	971.1	0.00326
165,000	392.4	0.00	0	0.00	2.41	3688	2.961	0.001790	971.1	0.00326
166,000	392.4	0.00	0	0.00	2.36	3668	2.961	0.001791	971.1	0.00326
167,000	392.4	0.00	0	0.00	2.31	3648	2.961	0.001792	971.1	0.00326
168,000	392.4	0.00	0	0.00	2.26	3628	2.961	0.001793	971.1	0.00326
169,000	392.4	0.00	0	0.00	2.21	3608	2.961	0.001794	971.1	0.00326
170,000	392.4	0.00	0	0.00	2.16	3588	2.961	0.001795		

TABLE III.—PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN ARBITRARY  
CONSTANT VALUE OF GRAVITATIONAL FORCE — BRITISH ENGINEERING SYSTEM — Continued

Altitude, h (ft)	Absolute tempera- ture, T (°F abs.)	Pressure, p (lb/ft <sup>2</sup> )	Pressure ratio, p/p <sub>0</sub>	Density, ρ (slugs/ft <sup>3</sup> )	Density ratio, σ = $\frac{\rho}{\rho_0}$	Specific weight, w = gP (lb/ft <sup>3</sup> )	Coefficient of viscosity, $\mu$ (lb sec/ft <sup>2</sup> ) (1)	Kinematic viscosity, $\nu = \frac{\mu}{\rho}$ (ft <sup>2</sup> /sec) (1)	Speed of sound, a (ft/sec)	Mean free path of molecules, λ (ft)
(b) For day only										
262,467	432.0	0.06669	3.151x10 <sup>-5</sup>	89.93x10 <sup>-9</sup>	3.782x10 <sup>-5</sup>	2.893x10 <sup>-6</sup>	3.212x10 <sup>-7</sup>	3.572	1019	6.40x10 <sup>-3</sup>
264,000	432.0	0.06241	2.949	83.75	3.522	2.695	3.212	3.835	1022	6.84
266,000	432.0	0.05724	2.705	76.33	3.210	2.456	3.212	4.208	1026	7.45
268,000	432.0	0.05257	2.484	69.65	2.929	2.241	3.212	4.612	1030	8.12
270,000	432.0	0.04829	2.282	63.59	2.674	2.046	3.212	5.051	1034	8.83
272,000	432.0	0.04438	2.097	58.07	2.442	1.868	3.212	5.531	1038	9.61
274,309	432.0	0.04081	2.070	57.26	2.408	1.842	3.212	5.610	1038	9.74
274,000	435.4	0.04082	1.929	52.67	2.215	1.695	3.232	5.136	1046	10.3
276,000	435.4	0.03760	1.776	47.77	2.009	1.537	3.257	6.818	1054	11.5
276,000	443.4	0.03469	1.638	43.42	1.826	1.397	3.282	7.559	1063	12.6
280,000	447.4	0.03200	1.512	39.45	1.659	1.269	3.306	8.380	1072	13.8
282,000	451.4	0.02956	1.397	35.91	1.510	1.155	3.331	9.273	1081	15.1
284,000	455.4	0.02736	1.293	32.74	1.377	1.053	3.355	10.25	1089	16.4
286,000	459.4	0.02535	1.198	29.89	1.257	0.9616	3.379	11.30	1098	17.9
288,000	463.4	0.02351	1.111	27.32	1.149	0.8791	3.403	12.46	1107	19.5
290,000	467.4	0.02184	1.032	25.02	1.052	0.8048	3.427	13.70	1116	21.1
292,000	471.4	0.02029	0.9588	22.91	0.9635	0.7371	3.451	15.06	1124	22.9
294,000	475.4	0.01888	0.8920	21.01	0.8837	0.6761	3.475	16.54	1133	24.9
296,000	479.4	0.01759	0.8310	19.30	0.8117	0.6210	3.499	18.13	1142	26.9
298,000	483.4	0.01639	0.7746	17.74	0.7460	0.5707	3.523	19.86	1151	29.1
300,000	487.4	0.01530	0.7228	16.32	0.6865	0.5252	3.546	21.73	1160	31.5
302,000	491.4	0.01428	0.6750	15.03	0.6322	0.4837	3.569	23.75	1169	34.0
304,000	495.4	0.01336	0.6314	13.87	0.5833	0.4463	3.593	25.90	1177	36.6
306,000	499.4	0.01250	0.5908	12.80	0.5384	0.4119	3.616	28.25	1186	39.4
308,000	503.4	0.01170	0.5531	11.82	0.4972	0.3804	3.639	30.79	1195	42.5
310,000	507.4	0.01098	0.5185	10.94	0.4599	0.3519	3.662	33.47	1204	45.7
312,000	511.5	0.01030	0.4866	10.13	0.4259	0.3258	3.685	36.38	1213	49.0
314,000	515.5	0.009671	0.4570	9.386	0.3947	0.3020	3.708	39.51	1222	52.6
316,000	519.5	0.009091	0.4296	8.705	0.3661	0.2801	3.731	42.86	1231	56.4
318,000	523.5	0.008550	0.4040	8.082	0.3399	0.2600	3.754	46.45	1240	60.5
320,000	527.5	0.008050	0.3804	7.509	0.3158	0.2416	3.777	50.30	1248	64.7
322,000	531.5	0.007585	0.3584	6.984	0.2937	0.2247	3.799	54.40	1257	69.2
324,000	535.5	0.007153	0.3380	6.504	0.2735	0.2092	3.822	58.75	1266	73.9
326,000	539.5	0.006744	0.3187	6.054	0.2546	0.1948	3.844	63.50	1275	79.0
328,000	543.5	0.006368	0.3009	5.645	0.2374	0.1816	3.867	68.48	1284	84.3
328,083	543.6	0.006353	0.3002	5.628	0.2367	0.1811	3.867	68.71	1285	84.5
330,000	547.5	0.006012	0.2841	5.288	0.2224	0.1701	3.889	73.54	1289	89.9
332,000	551.5	0.005686	0.2687	4.965	0.2088	0.1597	3.911	78.77	1294	95.8
334,000	555.5	0.005377	0.2541	4.661	0.1960	0.1500	3.933	84.38	1298	102
336,000	559.5	0.005087	0.2404	4.380	0.1842	0.1409	3.955	90.30	1303	109
338,000	563.5	0.004812	0.2274	4.114	0.1730	0.1324	3.977	96.67	1308	116
340,000	567.5	0.004556	0.2153	3.866	0.1626	0.1244	3.999	103.4	1312	123
342,000	571.5	0.004315	0.2039	3.636	0.1529	0.1170	4.021	110.5	1317	131
344,000	575.5	0.004091	0.1933	3.424	0.1440	0.1102	4.043	118.1	1322	139
346,000	579.5	0.003876	0.1831	3.220	0.1354	0.1036	4.065	126.2	1326	148
348,000	583.5	0.003674	0.1736	3.032	0.1275	0.09755	4.086	134.8	1331	157
350,000	587.5	0.003485	0.1647	2.858	0.1202	0.09196	4.108	143.7	1335	167
352,000	591.5	0.003306	0.1562	2.692	0.1132	0.08660	4.129	153.4	1340	177
354,000	595.5	0.003136	0.1482	2.537	0.1067	0.08163	4.151	163.6	1344	188
356,000	599.5	0.002978	0.1407	2.392	0.1006	0.07697	4.172	174.4	1349	199
358,000	603.5	0.002829	0.1337	2.258	0.09495	0.07264	4.193	185.7	1353	211
360,000	607.5	0.002690	0.1271	2.132	0.08967	0.06860	4.214	197.7	1358	223
362,000	611.5	0.002556	0.1208	2.013	0.08466	0.06477	4.236	210.4	1362	236
364,000	615.5	0.002429	0.1148	1.901	0.07994	0.06116	4.257	223.9	1367	250
366,000	619.5	0.002311	0.1092	1.796	0.07554	0.05779	4.278	238.2	1371	265
368,000	623.5	0.002199	0.1039	1.699	0.07142	0.05464	4.299	253.2	1376	280
370,000	627.5	0.002092	0.09887	1.606	0.06753	0.05165	4.319	268.9	1380	296
372,000	631.5	0.001992	0.09411	1.519	0.06387	0.04886	4.340	285.7	1384	313
374,000	635.5	0.001897	0.08952	1.437	0.06044	0.04624	4.361	303.5	1389	331
376,000	639.5	0.001806	0.08536	1.360	0.05720	0.04376	4.382	322.2	1393	350
378,000	643.6	0.001721	0.08133	1.288	0.05416	0.04144	4.402	341.8	1398	370
380,000	647.6	0.001640	0.07751	1.220	0.05130	0.03925	4.423	362.5	1402	390
382,000	651.6	0.001564	0.07390	1.156	0.04861	0.03719	4.443	384.3	1406	411
384,000	655.6	0.001492	0.07049	1.096	0.04609	0.03526	4.464	407.3	1411	434
386,000	659.6	0.001423	0.06724	1.039	0.04369	0.03343	4.484	431.6	1415	458
388,000	663.6	0.001358	0.06417	0.9856	0.04145	0.03171	4.504	457.0	1419	483
390,000	667.6	0.001296	0.06126	0.9352	0.03933	0.03009	4.525	483.9	1423	508
392,000	671.6	0.001237	0.05847	0.8872	0.03731	0.02854	4.545	512.3	1428	533
393,700	675.0	0.001190	0.05624	0.8491	0.03571	0.02732	4.562	537.3	1431	560

<sup>1</sup>The values for viscosity listed in these columns are not applicable at the higher altitudes where the mean free paths of the molecules are comparable to or longer than the dimensions of the body being considered. Furthermore, the values listed are based on the conventional Sutherland formula for normal air and, consequently, no allowance has been made for the effect of dissociated oxygen in the atmosphere at the higher levels.

TABLE III.—PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN ARBITRARY  
CONSTANT VALUE OF GRAVITATIONAL FORCE— BRITISH ENGINEERING SYSTEM— Concluded

Altitude, h (ft)	Absolute tempera- ture, T (°F abs.)	Pressure, p (lb/ft <sup>2</sup> )	Pressure ratio, p/p <sub>0</sub>	Density, ρ (slugs/ft <sup>3</sup> )	Density ratio, σ = $\frac{\rho}{\rho_0}$	Specific Weight, w = gρ (lb/ft <sup>3</sup> )	Coefficient of viscosity μ (lb-sec/ft <sup>2</sup> ) (1)	Kinematic viscosity, $\nu = \frac{\mu}{\rho}$ (ft <sup>2</sup> /sec) (1)	Speed of sound, a (ft/sec)	Mean free path of molecules, λ (ft)
(c) For night only										
262,467	432.0	0.06669	3.151×10 <sup>-5</sup>	89.93×10 <sup>-9</sup>	3.782×10 <sup>-5</sup>	2.893×10 <sup>-6</sup>	3.212×10 <sup>-7</sup>	3.572	1019	6.40×10 <sup>-3</sup>
264,000	432.0	0.06239	2.948	84.13	3.598	2.707	3.212	3.818	1019	6.84
266,000	432.0	0.05720	2.703	77.14	3.244	2.482	3.212	4.164	1019	7.46
268,000	432.0	0.05246	2.479	70.74	2.975	2.276	3.212	4.541	1019	8.13
270,000	432.0	0.04810	2.273	64.87	2.728	2.087	3.212	4.951	1019	8.87
272,000	432.0	0.04410	2.084	59.47	2.501	1.913	3.212	5.401	1019	9.67
272,309	432.0	0.04351	2.056	58.67	2.467	1.887	3.212	5.475	1019	9.80
274,000	435.4	0.04044	1.911	54.10	2.275	1.741	3.232	5.974	1023	10.6
276,000	439.4	0.03712	1.754	49.20	2.069	1.583	3.257	6.620	1028	11.7
278,000	443.4	0.03408	1.611	44.80	1.884	1.441	3.282	7.326	1032	12.8
280,000	447.4	0.03134	1.481	40.80	1.716	1.313	3.306	8.103	1037	14.1
282,000	451.4	0.02884	1.363	37.24	1.566	1.198	3.331	8.945	1042	15.5
284,000	455.4	0.02656	1.255	33.98	1.429	1.093	3.355	9.873	1046	16.9
286,000	459.4	0.02446	1.156	31.01	1.304	0.9976	3.379	10.90	1051	18.5
288,000	463.4	0.02256	1.066	28.34	1.192	0.9120	3.403	12.01	1055	20.3
290,000	467.4	0.02081	0.9832	25.92	1.090	0.8339	3.427	13.22	1060	22.2
292,000	471.4	0.01921	0.9079	23.74	0.9984	0.7638	3.451	14.54	1064	24.2
294,000	475.4	0.01774	0.8384	21.74	0.9142	0.6994	3.475	15.96	1069	26.5
296,000	479.4	0.01640	0.7748	19.92	0.8378	0.6410	3.499	17.57	1073	28.9
298,000	483.4	0.01517	0.7168	18.28	0.7687	0.5881	3.523	19.27	1078	31.5
300,000	487.4	0.01406	0.6643	16.80	0.7065	0.5405	3.546	21.11	1082	34.2
302,000	491.4	0.01302	0.6151	15.43	0.6489	0.4964	3.569	23.13	1087	37.3
304,000	495.4	0.01206	0.5699	14.18	0.5963	0.4562	3.593	25.34	1091	40.6
306,000	499.4	0.01119	0.5286	13.05	0.5487	0.4198	3.616	27.71	1096	44.1
308,000	503.4	0.01038	0.4906	12.01	0.5052	0.3865	3.639	30.30	1100	47.9
310,000	507.4	0.009642	0.4556	11.07	0.4654	0.3561	3.662	33.08	1104	52.0
312,000	511.5	0.008958	0.4233	10.20	0.4290	0.3282	3.685	36.13	1109	56.4
314,000	515.5	0.008327	0.3935	9.409	0.3957	0.3027	3.708	39.41	1113	61.1
316,000	519.5	0.007745	0.3660	8.686	0.3653	0.2795	3.731	42.95	1117	66.2
318,000	523.5	0.007210	0.3407	8.023	0.3374	0.2581	3.754	46.79	1122	71.7
320,000	527.5	0.006711	0.3171	7.410	0.3116	0.2384	3.777	50.97	1126	77.6
322,000	531.5	0.006253	0.2955	6.853	0.2882	0.2205	3.799	55.44	1130	83.9
324,000	535.5	0.005826	0.2753	6.337	0.2665	0.2039	3.822	60.31	1134	90.8
326,000	539.5	0.005437	0.2569	5.871	0.2469	0.1889	3.844	65.47	1139	98.0
328,000	543.5	0.005073	0.2397	5.436	0.2286	0.1749	3.867	71.14	1143	106
330,000	547.5	0.004736	0.2238	5.039	0.2119	0.1621	3.889	77.18	1147	114
332,000	551.5	0.004423	0.2090	4.673	0.1965	0.1503	3.911	83.69	1151	123
334,000	555.5	0.004133	0.1953	4.335	0.1823	0.1396	3.933	90.73	1155	133
336,000	559.5	0.003864	0.1826	4.023	0.1692	0.1294	3.955	98.31	1160	143
338,000	563.5	0.003617	0.1709	3.738	0.1572	0.1203	3.977	106.4	1164	154
340,000	567.5	0.003384	0.1599	3.474	0.1461	0.1118	3.999	115.1	1168	166
342,000	571.5	0.003166	0.1496	3.227	0.1357	0.1038	4.021	124.6	1172	178
344,000	575.5	0.002967	0.1402	3.003	0.1263	0.09663	4.043	134.6	1176	192
344,487	576.5	0.002920	0.1380	2.951	0.1241	0.09494	4.048	137.2	1177	195
346,000	579.5	0.002781	0.1314	2.777	0.1168	0.08936	4.065	146.4	1185	206
348,000	583.5	0.002611	0.1254	2.568	0.1080	0.08263	4.085	159.1	1195	221
350,000	587.5	0.002453	0.1199	2.376	0.09992	0.07644	4.108	172.9	1205	237
352,000	591.5	0.002305	0.1089	2.199	0.09248	0.07075	4.129	187.8	1215	253
354,000	595.5	0.002169	0.1025	2.039	0.08575	0.06560	4.151	203.6	1226	271
356,000	599.5	0.002041	0.09646	1.891	0.07951	0.06083	4.172	220.6	1236	290
358,000	603.5	0.001924	0.09090	1.756	0.07383	0.05748	4.193	238.8	1246	310
360,000	607.5	0.001815	0.08576	1.632	0.06864	0.05251	4.214	258.2	1256	331
362,000	611.5	0.001714	0.08098	1.519	0.06388	0.04887	4.236	278.9	1267	353
364,000	615.5	0.001618	0.07648	1.414	0.05947	0.04550	4.257	301.1	1277	376
366,000	619.6	0.001531	0.07235	1.319	0.05546	0.04243	4.278	324.3	1287	400
368,000	623.6	0.001449	0.06848	1.231	0.05175	0.03959	4.299	349.2	1297	425
370,000	627.6	0.001373	0.06488	1.149	0.04834	0.03698	4.319	375.9	1308	451
372,000	631.6	0.001302	0.06151	1.075	0.04520	0.03458	4.340	403.7	1318	479
374,000	635.6	0.001235	0.05836	1.006	0.04229	0.03235	4.361	433.5	1328	508
376,000	639.6	0.001172	0.05537	0.9409	0.03957	0.03027	4.382	465.7	1339	539
378,000	643.6	0.001113	0.05260	0.8817	0.03708	0.02837	4.402	499.3	1349	571
380,000	647.6	0.001058	0.05000	0.8268	0.03477	0.02660	4.423	535.0	1359	604
382,000	651.6	0.001007	0.04757	0.7761	0.03264	0.02497	4.443	572.5	1370	639
384,000	655.6	0.0009582	0.04528	0.7288	0.03065	0.02345	4.464	612.5	1381	676
386,000	659.6	0.0009127	0.04313	0.6851	0.02881	0.02204	4.484	654.5	1391	714
388,000	663.6	0.0008702	0.04112	0.6444	0.02710	0.02073	4.504	698.9	1401	754
390,000	667.6	0.0008296	0.03920	0.6064	0.02550	0.01951	4.525	746.2	1412	795
392,000	671.6	0.0007917	0.03741	0.5712	0.02402	0.01838	4.545	795.7	1422	838
393,700	675.0	0.0007614	0.03598	0.5434	0.02285	0.01748	4.562	839.5	1431	875

<sup>1</sup>The values for viscosity listed in these columns are not applicable at the higher altitudes where the mean free paths of the molecules are comparable to or longer than the dimensions of the body being considered. Furthermore, the values listed are based on the conventional Sutherland formula for normal air and, consequently, no allowance has been made for the effect of dissociated oxygen in the atmosphere at the higher levels.

## TABLES IV AND V

PROPERTIES OF THE UPPER ATMOSPHERE  
FOR TENTATIVE STANDARD TEMPERATURES  
BASED ON AN INVERSE SQUARE VARIATION  
OF GRAVITATIONAL FORCE

The following set of two tables (tables IV and V) does not constitute a consistent extension of the standard tables for the lower atmosphere (NACA Rep. No. 218) but takes into account the inverse square law of gravitational attraction and, consequently, the values in these tables are more accurate than those in tables II and III.

NATIONAL ADVISORY  
COMMITTEE FOR AERONAUTICS.





TABLE II.— PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN  
INVERSE SQUARE VARIATION OF GRAVITATIONAL FORCE — METRIC ENGINEERING SYSTEM — Concluded

Altitude, h (m)	Absolute temperature, T (°K)	Pressure, p (kg/m <sup>2</sup> )	Pressure ratio, p/p <sub>0</sub>	Density, $\rho$ (kg/m <sup>3</sup> )	Density ratio, $\sigma = \frac{\rho}{\rho_0}$	Specific weight, $\gamma = \frac{\rho}{\rho_0}$ (kg/m <sup>3</sup> )	Coefficient of viscosity, $\mu$ ( $\frac{\text{kg-sec}}{\text{m}^2}$ )	Kinematic viscosity, $\nu = \frac{\mu}{\rho}$ (m <sup>2</sup> /sec) (1)	Speed of sound, a (m/sec)	Mean free path of molecules, $\lambda$ (m)
(b) For day only										
80,000	240.0	0.3575	3557 $\times 10^{-8}$	5334 $\times 10^{-9}$	4268 $\times 10^{-8}$	5102 $\times 10^{-8}$	1.568 $\times 10^{-6}$	0.2940	310.6	1.68 $\times 10^{-3}$
81,000	240.0	0.3201	3096	4598	3680	4395	1.568	0.3411	312.5	1.93
82,000	240.0	0.2793	2703	3970	3177	3795	1.568	0.3950	314.5	2.22
83,000	240.0	0.2439	2361	3432	2744	3260	1.568	0.4568	316.5	2.54
84,000	243.6	0.2136	2067	2931	2345	2800	1.568	0.5415	320.8	2.94
85,000	247.3	0.1877	1817	2513	2011	2399	1.607	0.6394	325.3	3.39
86,000	250.9	0.1653	1600	2163	1729	2062	1.627	0.7529	329.6	3.91
87,000	254.6	0.1415	1369	1849	1492	1779	1.645	0.8827	333.9	4.48
88,000	258.2	0.1243	1203	1614	1292	1540	1.666	1.031	338.3	5.12
89,000	261.9	0.1153	1116	1402	1122	1337	1.685	1.202	342.7	5.84
90,000	265.5	0.1029	995.6	1222	977.5	1165	1.704	1.395	347.1	6.64
91,000	269.2	0.09195	890.0	1067	853.8	1017	1.723	1.614	351.5	7.52
92,000	272.8	0.08244	797.9	935.1	748.3	891.0	1.742	1.862	355.9	8.50
93,000	276.5	0.07406	717.0	821.3	657.3	782.8	1.760	2.143	360.4	9.59
94,000	280.1	0.06656	645.7	723.0	579.0	689.2	1.779	2.459	364.9	10.8
95,000	283.8	0.06023	583.0	651.3	513.3	604.5	1.797	2.814	369.3	12.1
96,000	287.4	0.05453	527.8	585.8	452.8	538.8	1.816	3.208	373.7	13.5
97,000	291.1	0.04945	478.6	502.2	401.9	478.0	1.834	3.652	378.1	15.1
98,000	294.7	0.04494	435.0	446.9	357.6	425.1	1.852	4.145	382.6	16.8
99,000	298.4	0.04093	396.1	398.5	318.8	378.9	1.870	4.694	387.1	18.7
100,000	302.0	0.03734	361.4	356.0	284.9	338.4	1.888	5.303	391.5	20.7
101,000	305.7	0.03412	330.2	321.4	257.7	305.5	1.906	6.028	395.9	23.0
102,000	309.3	0.03122	302.1	290.6	232.6	276.1	1.924	6.816	399.3	25.6
103,000	313.0	0.02859	276.7	263.1	210.5	249.9	1.941	7.735	402.8	28.0
104,000	316.6	0.02621	253.7	238.4	190.8	226.4	1.959	8.810	406.9	30.9
105,000	320.3	0.02406	232.8	216.3	173.1	205.3	1.976	9.129	409.2	34.1
106,000	323.9	0.02210	213.9	196.5	157.2	186.4	1.994	10.14	409.5	37.5
107,000	327.6	0.02032	196.7	178.7	143.0	169.5	2.011	11.24	407.7	41.2
108,000	331.2	0.01870	181.0	162.7	130.2	154.2	2.028	12.46	410.0	45.3
109,000	334.9	0.01723	166.8	148.2	118.6	140.5	2.045	13.79	412.3	49.7
110,000	338.5	0.01589	153.8	135.2	108.2	128.1	2.062	15.24	414.5	54.4
111,000	342.2	0.01466	141.9	123.5	98.79	117.0	2.079	16.83	416.7	59.6
112,000	345.8	0.01355	131.1	113.8	90.29	106.9	2.096	18.56	418.9	65.2
113,000	349.5	0.01252	121.2	103.2	82.62	97.75	2.113	20.45	421.1	71.2
114,000	353.1	0.01159	112.2	94.55	75.66	89.49	2.129	22.51	423.3	77.8
115,000	356.8	0.01074	103.9	86.66	69.34	82.00	2.146	24.75	425.5	84.5
116,000	360.4	0.009947	96.27	79.50	63.62	75.21	2.162	27.19	427.7	91.4
117,000	364.1	0.009227	89.30	72.00	58.41	69.03	2.179	29.83	429.8	101
118,000	367.7	0.008565	82.90	64.71	53.69	63.43	2.195	32.71	432.0	109
119,000	371.4	0.007958	77.02	61.72	49.38	58.33	2.211	35.82	434.1	119
120,000	375.0	0.007398	71.60	56.82	45.46	53.67	2.227	39.20	436.3	129
(c) For night only										
80,000	240.0	0.3575	3557 $\times 10^{-8}$	5334 $\times 10^{-9}$	4268 $\times 10^{-8}$	5102 $\times 10^{-8}$	1.568 $\times 10^{-6}$	0.2940	310.6	1.68 $\times 10^{-3}$
81,000	240.0	0.3198	3096	4641	3713	4439	1.568	0.3377	310.6	1.93
82,000	240.0	0.2784	2695	4041	3233	3861	1.568	0.3870	310.6	2.22
83,000	240.0	0.2448	2348	3518	2818	3363	1.568	0.4428	312.9	2.57
84,000	243.6	0.2112	2044	3020	2412	2885	1.588	0.5269	316.9	2.97
85,000	247.3	0.1844	1785	2598	2079	2481	1.607	0.6189	321.3	3.45
86,000	250.9	0.1613	1562	2240	1793	2138	1.627	0.7265	325.6	4.00
87,000	254.6	0.1415	1369	1936	1549	1847	1.645	0.8499	329.9	4.63
88,000	258.2	0.1243	1203	1675	1341	1599	1.666	0.9939	334.2	5.34
89,000	261.9	0.1094	1058	1455	1164	1387	1.685	1.158	338.4	6.16
90,000	265.5	0.09540	933.0	1265	1012	1206	1.704	1.347	342.7	7.08
91,000	269.2	0.08315	824.1	1101	881.1	1050	1.723	1.564	346.9	8.12
92,000	272.8	0.07333	729.1	961.8	769.6	916.4	1.742	1.811	351.1	9.31
93,000	276.5	0.06676	648.1	841.1	673.1	801.2	1.760	2.093	355.4	10.6
94,000	280.1	0.05926	573.5	737.0	589.7	701.8	1.779	2.414	359.5	12.1
95,000	283.8	0.05269	509.9	646.7	517.5	615.6	1.798	2.780	363.7	13.8
96,000	287.4	0.04691	454.0	568.2	454.9	541.1	1.816	3.195	367.9	15.7
97,000	291.1	0.04183	404.9	500.6	400.5	476.3	1.834	3.664	372.0	17.9
98,000	294.7	0.03736	361.6	441.5	353.3	420.0	1.852	4.196	376.1	20.2
99,000	298.4	0.03341	323.3	390.0	312.1	370.9	1.870	4.795	380.2	22.9
100,000	302.0	0.02992	289.5	345.0	276.1	328.0	1.888	5.472	384.3	25.9
101,000	305.7	0.02683	259.7	305.8	244.7	290.6	1.906	6.233	388.4	29.2
102,000	309.3	0.02409	233.2	271.3	217.1	257.8	1.924	7.090	392.5	32.9
103,000	313.0	0.02166	209.7	241.1	192.9	229.0	1.942	8.052	396.7	37.0
104,000	316.6	0.01950	188.6	214.5	173.0	203.7	1.959	9.130	399.7	41.6
105,000	320.3	0.01758	170.2	193.2	153.6	183.5	1.976	10.34	402.8	46.6
106,000	323.9	0.01588	153.7	173.1	134.8	160.8	1.994	11.84	405.9	52.1
107,000	327.6	0.01438	139.7	158.7	119.0	143.0	2.011	13.52	408.9	58.3
108,000	331.2	0.01305	128.3	143.7	105.4	124.8	2.028	15.41	411.9	64.9
109,000	334.9	0.01187	114.9	126.9	93.57	110.8	2.045	17.49	414.9	72.1
110,000	338.5	0.01082	104.8	104.1	83.30	98.63	2.062	19.81	417.9	79.9
111,000	342.2	0.00990	95.72	92.90	74.33	87.90	2.079	22.38	420.9	88.4
112,000	345.8	0.009059	87.68	83.11	66.20	78.70	2.096	25.24	423.9	97.2
113,000	349.5	0.008345	80.47	75.00	59.25	70.50	2.113	28.32	426.9	107
114,000	353.1	0.007746	74.00	66.99	53.60	63.40	2.129	31.78	429.9	118
115,000	356.8	0.007242	68.15	60.33	48.28	57.09	2.146	35.57	432.9	129
116,000	360.4	0.006799	62.90	54.44	43.56	51.49	2.162	39.72	435.9	141
117,000	364.1	0.006409	58.16	49.24	39.40	46.55	2.179	44.25	438.9	154
118,000	367.7	0.005967	53.88	44.63	35.71	42.18	2.195	49.18	441.9	168
119,000	371.4	0.005564	49.98	40.50	32.41	38.26	2.211	54.58	444.9	183
120,000	375.0	0.004800	46.45	36.86	29.50	34.82	2.227	60.42	447.9	199

<sup>1</sup> The values for viscosity listed in these columns are not applicable at the higher altitudes where the mean free paths of the molecules are comparable to or longer than the dimensions of the body being considered. Furthermore, the values listed are based on the conventional Sutherland formula for normal air and, consequently, no allowance has been made for the effect of dissociated oxygen in the atmosphere at the higher levels.

TABLE V.—PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN INVERSE SQUARE VARIATION OF GRAVITATIONAL FORCE—BRITISH ENGINEERING SYSTEM

Altitude, (ft)	Absolute temperature, (°C abs.)	Pressure, (lb./ft. <sup>2</sup> )	Pressure ratio, P/P <sub>0</sub>	Density, ρ (slugs/ft. <sup>3</sup> )	Density ratio, ρ/ρ <sub>0</sub>	Specific weight, γ = ρg (lb./ft. <sup>3</sup> )	Coefficient of viscosity, μ (lb.-sec/ft. <sup>2</sup> )	Kinematic viscosity, ν = μ/ρ (ft. <sup>2</sup> /sec)	Speed of sound, a (ft./sec)	Mean free path of molecules, λ (ft.)
(a) For both day and night										
64,000	392.4	119.9	265.4×10 <sup>-5</sup>	1.779×10 <sup>-7</sup>	7.483×10 <sup>-5</sup>	2.961×10 <sup>-6</sup>	0.001563	971.1	0.00327×10 <sup>-3</sup>	
65,000	392.4	117.5	260.2	1.757	7.357	2.961	0.001578	971.1	0.00337	
66,000	392.4	115.0	255.1	1.734	7.232	2.961	0.001593	971.1	0.00347	
67,000	392.4	112.6	250.0	1.711	7.107	2.961	0.001608	971.1	0.00357	
68,000	392.4	110.1	244.9	1.688	6.982	2.961	0.001623	971.1	0.00367	
69,000	392.4	107.7	239.8	1.665	6.857	2.961	0.001638	971.1	0.00377	
70,000	392.4	105.3	234.7	1.642	6.732	2.961	0.001653	971.1	0.00387	
71,000	392.4	102.8	229.6	1.619	6.607	2.961	0.001668	971.1	0.00397	
72,000	392.4	100.4	224.5	1.596	6.482	2.961	0.001683	971.1	0.00407	
73,000	392.4	97.9	219.4	1.573	6.357	2.961	0.001698	971.1	0.00417	
74,000	392.4	95.5	214.3	1.550	6.232	2.961	0.001713	971.1	0.00427	
75,000	392.4	93.0	209.2	1.527	6.107	2.961	0.001728	971.1	0.00437	
76,000	392.4	90.6	204.1	1.504	5.982	2.961	0.001743	971.1	0.00447	
77,000	392.4	88.1	199.0	1.481	5.857	2.961	0.001758	971.1	0.00457	
78,000	392.4	85.7	193.9	1.458	5.732	2.961	0.001773	971.1	0.00467	
79,000	392.4	83.2	188.8	1.435	5.607	2.961	0.001788	971.1	0.00477	
80,000	392.4	80.8	183.7	1.412	5.482	2.961	0.001803	971.1	0.00487	
81,000	392.4	78.3	178.6	1.389	5.357	2.961	0.001818	971.1	0.00497	
82,000	392.4	75.9	173.5	1.366	5.232	2.961	0.001833	971.1	0.00507	
83,000	392.4	73.4	168.4	1.343	5.107	2.961	0.001848	971.1	0.00517	
84,000	392.4	71.0	163.3	1.320	4.982	2.961	0.001863	971.1	0.00527	
85,000	392.4	68.5	158.2	1.297	4.857	2.961	0.001878	971.1	0.00537	
86,000	392.4	66.1	153.1	1.274	4.732	2.961	0.001893	971.1	0.00547	
87,000	392.4	63.6	148.0	1.251	4.607	2.961	0.001908	971.1	0.00557	
88,000	392.4	61.2	142.9	1.228	4.482	2.961	0.001923	971.1	0.00567	
89,000	392.4	58.7	137.8	1.205	4.357	2.961	0.001938	971.1	0.00577	
90,000	392.4	56.3	132.7	1.182	4.232	2.961	0.001953	971.1	0.00587	
91,000	392.4	53.8	127.6	1.159	4.107	2.961	0.001968	971.1	0.00597	
92,000	392.4	51.4	122.5	1.136	3.982	2.961	0.001983	971.1	0.00607	
93,000	392.4	48.9	117.4	1.113	3.857	2.961	0.001998	971.1	0.00617	
94,000	392.4	46.5	112.3	1.090	3.732	2.961	0.002013	971.1	0.00627	
95,000	392.4	44.0	107.2	1.067	3.607	2.961	0.002028	971.1	0.00637	
96,000	392.4	41.6	102.1	1.044	3.482	2.961	0.002043	971.1	0.00647	
97,000	392.4	39.1	97.0	1.021	3.357	2.961	0.002058	971.1	0.00657	
98,000	392.4	36.7	91.9	1.000	3.232	2.961	0.002073	971.1	0.00667	
99,000	392.4	34.2	86.8	0.977	3.107	2.961	0.002088	971.1	0.00677	
100,000	392.4	31.8	81.7	0.954	2.982	2.961	0.002103	971.1	0.00687	
101,000	392.4	29.3	76.6	0.931	2.857	2.961	0.002118	971.1	0.00697	
102,000	392.4	26.9	71.5	0.908	2.732	2.961	0.002133	971.1	0.00707	
103,000	392.4	24.4	66.4	0.885	2.607	2.961	0.002148	971.1	0.00717	
104,000	392.4	22.0	61.3	0.862	2.482	2.961	0.002163	971.1	0.00727	
105,000	392.4	19.5	56.2	0.839	2.357	2.961	0.002178	971.1	0.00737	
106,000	392.4	17.1	51.1	0.816	2.232	2.961	0.002193	971.1	0.00747	
107,000	392.4	14.6	46.0	0.793	2.107	2.961	0.002208	971.1	0.00757	
108,000	392.4	12.2	40.9	0.770	1.982	2.961	0.002223	971.1	0.00767	
109,000	392.4	9.7	35.8	0.747	1.857	2.961	0.002238	971.1	0.00777	
110,000	392.4	7.3	30.7	0.724	1.732	2.961	0.002253	971.1	0.00787	
111,000	392.4	4.8	25.6	0.701	1.607	2.961	0.002268	971.1	0.00797	
112,000	392.4	2.3	20.5	0.678	1.482	2.961	0.002283	971.1	0.00807	
113,000	392.4	0.0	15.4	0.655	1.357	2.961	0.002298	971.1	0.00817	
114,000	392.4	0.0	10.3	0.632	1.232	2.961	0.002313	971.1	0.00827	
115,000	392.4	0.0	5.2	0.609	1.107	2.961	0.002328	971.1	0.00837	
116,000	392.4	0.0	0.1	0.586	0.982	2.961	0.002343	971.1	0.00847	
117,000	392.4	0.0	0.0	0.563	0.857	2.961	0.002358	971.1	0.00857	
118,000	392.4	0.0	0.0	0.540	0.732	2.961	0.002373	971.1	0.00867	
119,000	392.4	0.0	0.0	0.517	0.607	2.961	0.002388	971.1	0.00877	
120,000	392.4	0.0	0.0	0.494	0.482	2.961	0.002403	971.1	0.00887	
121,000	392.4	0.0	0.0	0.471	0.357	2.961	0.002418	971.1	0.00897	
122,000	392.4	0.0	0.0	0.448	0.232	2.961	0.002433	971.1	0.00907	
123,000	392.4	0.0	0.0	0.425	0.107	2.961	0.002448	971.1	0.00917	
124,000	392.4	0.0	0.0	0.402	0.0	2.961	0.002463	971.1	0.00927	
125,000	392.4	0.0	0.0	0.379	0.0	2.961	0.002478	971.1	0.00937	
126,000	392.4	0.0	0.0	0.356	0.0	2.961	0.002493	971.1	0.00947	
127,000	392.4	0.0	0.0	0.333	0.0	2.961	0.002508	971.1	0.00957	
128,000	392.4	0.0	0.0	0.310	0.0	2.961	0.002523	971.1	0.00967	
129,000	392.4	0.0	0.0	0.287	0.0	2.961	0.002538	971.1	0.00977	
130,000	392.4	0.0	0.0	0.264	0.0	2.961	0.002553	971.1	0.00987	
131,000	392.4	0.0	0.0	0.241	0.0	2.961	0.002568	971.1	0.00997	
132,000	392.4	0.0	0.0	0.218	0.0	2.961	0.002583	971.1	0.01007	
133,000	392.4	0.0	0.0	0.195	0.0	2.961	0.002598	971.1	0.01017	
134,000	392.4	0.0	0.0	0.172	0.0	2.961	0.002613	971.1	0.01027	
135,000	392.4	0.0	0.0	0.149	0.0	2.961	0.002628	971.1	0.01037	
136,000	392.4	0.0	0.0	0.126	0.0	2.961	0.002643	971.1	0.01047	
137,000	392.4	0.0	0.0	0.103	0.0	2.961	0.002658	971.1	0.01057	
138,000	392.4	0.0	0.0	0.080	0.0	2.961	0.002673	971.1	0.01067	
139,000	392.4	0.0	0.0	0.057	0.0	2.961	0.002688	971.1	0.01077	
140,000	392.4	0.0	0.0	0.034	0.0	2.961	0.002703	971.1	0.01087	
141,000	392.4	0.0	0.0	0.011	0.0	2.961	0.002718	971.1	0.01097	
142,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002733	971.1	0.01107	
143,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002748	971.1	0.01117	
144,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002763	971.1	0.01127	
145,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002778	971.1	0.01137	
146,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002793	971.1	0.01147	
147,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002808	971.1	0.01157	
148,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002823	971.1	0.01167	
149,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002838	971.1	0.01177	
150,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002853	971.1	0.01187	
151,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002868	971.1	0.01197	
152,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002883	971.1	0.01207	
153,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002898	971.1	0.01217	
154,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002913	971.1	0.01227	
155,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002928	971.1	0.01237	
156,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002943	971.1	0.01247	
157,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002958	971.1	0.01257	
158,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002973	971.1	0.01267	
159,000	392.4	0.0	0.0	0.0	0.0	2.961	0.002988	971.1	0.01277	
160,000	392.4	0.0	0.0	0.0	0.0	2.961	0.003003	971.1	0.01287	
161,000	392.4	0.0	0.0	0.0	0.0	2.961	0.003018	971.1	0.01297	
162,000	392.4	0.0	0.0	0.0	0.0	2.961	0.003033	971.1	0.01307	
163,000	392.4	0.0	0.0	0.0	0.0	2.961	0.003048	971.1	0.01317	
164,000	392.4	0.0	0.0	0.0	0.0	2.961	0.003063	971.1	0.01327	
165,000	392.4	0.0	0.0	0.0	0.0	2.961	0.003078	971.1	0.01337	
166,000	392.4	0.0	0.0	0.0	0.0	2.961	0.003093	971.1	0.01347	
167,000	392.4	0.0	0.0	0.0	0.0	2.961	0.003108	971.1	0.01357	
168,000	392.4	0.0	0.0	0.0	0.0	2.961	0.003123	971.1	0.01367	
169,000	392.4	0.0	0.0	0.0	0.0	2.961	0.003138	971.1		



TABLE Y. — PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN  
INVERSE SQUARE VARIATION OF GRAVITATIONAL FORCE — BRITISH ENGINEERING SYSTEM — Continued

Altitude, h (ft)	Absolute tempera- ture, T (°F abs.)	Pressure, p (lb/ft <sup>2</sup> )	Pressure ratio, p/p <sub>0</sub>	Density, ρ (slugs/ft <sup>3</sup> )	Density ratio, σ = ρ/ρ <sub>0</sub>	Specific weight, γ = ρg (lb/ft <sup>3</sup> )	Coefficient of viscosity, μ (lb-sec/ft <sup>2</sup> ) (1)	Kinematic viscosity, ν = μ/ρ (ft <sup>2</sup> /sec) (1)	Speed of sound, a (ft/sec)	Mean free path of molecules, λ (ft)
(b) For day only										
262,467	432.0	0.07527	3.557×10 <sup>-5</sup>	101.5×10 <sup>-9</sup>	4.268×10 <sup>-5</sup>	3.185×10 <sup>-6</sup>	3.212×10 <sup>-7</sup>	3.165	1019	5.53×10 <sup>-3</sup>
264,000	432.0	0.07056	3.334	94.66	3.981	2.970	3.212	3.392	1022	5.90
266,000	432.0	0.06484	3.064	86.46	3.636	2.712	3.212	3.715	1026	6.42
268,000	432.0	0.05968	2.820	79.07	3.325	2.430	3.212	4.062	1030	6.97
270,000	432.0	0.05494	2.596	72.34	3.042	2.268	3.212	4.440	1034	7.57
272,000	432.0	0.05060	2.391	66.32	2.784	2.076	3.212	4.852	1038	8.22
274,000	432.0	0.04666	2.204	60.18	2.531	1.887	3.232	5.371	1046	8.98
276,000	439.4	0.04302	2.033	54.67	2.299	1.713	3.257	5.958	1054	9.82
278,000	443.4	0.03972	1.877	49.72	2.091	1.558	3.282	6.601	1063	10.7
280,000	447.4	0.03678	1.738	45.35	1.907	1.421	3.306	7.290	1072	11.7
282,000	451.4	0.03409	1.611	41.42	1.742	1.297	3.331	8.042	1081	12.7
284,000	455.4	0.03160	1.493	37.81	1.590	1.184	3.355	8.873	1089	13.9
286,000	459.4	0.02933	1.386	34.60	1.455	1.083	3.379	9.766	1098	15.1
288,000	463.4	0.02726	1.288	31.67	1.332	0.9915	3.403	10.75	1107	16.3
290,000	467.4	0.02537	1.199	29.06	1.222	0.9095	3.427	11.79	1116	17.7
292,000	471.4	0.02362	1.116	26.66	1.121	0.8342	3.451	12.94	1124	19.2
294,000	475.4	0.02201	1.040	24.49	1.030	0.7663	3.475	14.19	1133	20.7
296,000	479.4	0.02055	0.9710	22.55	0.9484	0.7054	3.499	15.52	1142	22.4
298,000	483.4	0.01919	0.9069	20.77	0.8734	0.6495	3.522	16.96	1151	24.2
300,000	487.4	0.01794	0.8479	19.15	0.8053	0.5988	3.546	18.52	1160	26.1
302,000	491.4	0.01679	0.7933	17.67	0.7430	0.5524	3.569	20.24	1168	28.1
304,000	495.4	0.01573	0.7435	16.33	0.6869	0.5105	3.593	22.00	1177	30.2
306,000	499.4	0.01475	0.6970	15.10	0.6352	0.4720	3.616	23.95	1186	32.5
308,000	503.4	0.01383	0.6537	13.97	0.5877	0.4366	3.639	26.05	1196	34.9
310,000	507.4	0.01299	0.6140	12.95	0.5446	0.4046	3.662	28.28	1204	37.4
312,000	511.5	0.01221	0.5772	12.01	0.5051	0.3751	3.685	30.68	1213	40.1
314,000	515.5	0.01149	0.5431	11.15	0.4690	0.3482	3.708	33.26	1222	43.0
316,000	519.5	0.01082	0.5114	10.37	0.4359	0.3236	3.731	35.98	1231	46.0
318,000	523.5	0.01020	0.4819	9.640	0.4054	0.3009	3.754	38.94	1240	49.2
320,000	527.5	0.009620	0.4546	8.977	0.3775	0.2802	3.777	42.07	1248	52.5
322,000	531.5	0.009079	0.4290	8.361	0.3516	0.2609	3.799	45.44	1257	56.1
324,000	535.5	0.008579	0.4054	7.800	0.3280	0.2434	3.822	49.00	1266	59.8
326,000	539.5	0.008103	0.3829	7.274	0.3059	0.2269	3.844	52.85	1275	63.7
328,000	543.5	0.007663	0.3621	6.791	0.2856	0.2118	3.867	56.94	1284	67.9
328,083	543.6	0.007648	0.3614	6.775	0.2849	0.2113	3.867	57.06	1285	68.0
330,000	547.5	0.007243	0.3425	6.375	0.2661	0.1968	3.889	61.00	1293	72.8
332,000	551.5	0.006867	0.3245	5.997	0.2502	0.1871	3.911	65.22	1304	76.8
334,000	555.5	0.006505	0.3074	5.640	0.2372	0.1758	3.933	69.77	1315	81.7
336,000	559.5	0.006167	0.2914	5.307	0.2232	0.1654	3.955	74.52	1326	86.8
338,000	563.5	0.005843	0.2761	4.994	0.2100	0.1556	3.977	79.64	1338	92.2
340,000	567.5	0.005540	0.2618	4.701	0.1977	0.1464	3.999	85.07	1349	97.9
342,000	571.5	0.005257	0.2484	4.430	0.1863	0.1379	4.021	90.77	1361	104
344,000	575.5	0.004992	0.2359	4.178	0.1757	0.1301	4.043	96.77	1372	110
346,000	579.5	0.004736	0.2238	3.935	0.1655	0.1226	4.065	103.3	1386	117
348,000	583.5	0.004499	0.2126	3.714	0.1562	0.1156	4.086	110.0	1399	124
350,000	587.5	0.004275	0.2020	3.505	0.1474	0.1091	4.108	117.2	1413	131
352,000	591.5	0.004061	0.1919	3.305	0.1390	0.1029	4.129	124.9	1428	139
354,000	595.5	0.003860	0.1824	3.122	0.1313	0.09716	4.151	133.0	1444	147
356,000	599.5	0.003672	0.1735	2.949	0.1240	0.09173	4.172	141.5	1461	156
358,000	603.5	0.003494	0.1651	2.787	0.1172	0.08668	4.193	150.4	1479	165
360,000	607.5	0.003329	0.1573	2.637	0.1110	0.08205	4.214	159.8	1498	174
362,000	611.5	0.003168	0.1497	2.494	0.1049	0.07778	4.236	169.8	1518	184
364,000	615.5	0.003016	0.1425	2.359	0.0992	0.07383	4.257	180.4	1539	194
366,000	619.5	0.002874	0.1358	2.234	0.09395	0.06942	4.278	191.5	1561	205
368,000	623.6	0.002738	0.1294	2.115	0.08894	0.06571	4.299	203.3	1584	217
370,000	627.6	0.002611	0.1234	2.004	0.08428	0.06225	4.319	215.6	1608	229
372,000	631.6	0.002489	0.1176	1.898	0.07981	0.05894	4.340	228.7	1634	242
374,000	635.6	0.002374	0.1122	1.799	0.07566	0.05586	4.361	242.4	1661	255
376,000	639.6	0.002266	0.1071	1.707	0.07177	0.05298	4.382	256.7	1689	269
378,000	643.6	0.002163	0.1022	1.618	0.06806	0.05023	4.402	272.1	1718	283
380,000	647.6	0.002064	0.09754	1.535	0.06456	0.04764	4.423	288.1	1748	299
382,000	651.6	0.001971	0.09316	1.457	0.06128	0.04522	4.443	304.9	1779	315
384,000	655.6	0.001884	0.08901	1.384	0.05819	0.04293	4.464	322.5	1811	331
386,000	659.6	0.001800	0.08505	1.314	0.05527	0.04076	4.484	341.2	1845	349
388,000	663.6	0.001721	0.08131	1.249	0.05252	0.03873	4.504	360.6	1881	367
390,000	667.6	0.001646	0.07776	1.187	0.04992	0.03681	4.525	381.2	1918	386
392,000	671.6	0.001573	0.07434	1.128	0.04744	0.03497	4.545	402.9	1956	406
393,700	675.0	0.001515	0.07160	1.081	0.04546	0.03350	4.562	422.0	1993	424

<sup>1</sup>The values for viscosity listed in these columns are not applicable at the higher altitudes where the mean free paths of the molecules are comparable to or longer than the dimensions of the body being considered. Furthermore, the values listed are based on the conventional Sutherland formula for normal air and, consequently, no allowance has been made for the effect of dissociated oxygen in the atmosphere at the higher levels.

TABLE V.- PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN  
INVERSE SQUARE VARIATION OF GRAVITATIONAL FORCE- BRITISH ENGINEERING SYSTEM- Concluded

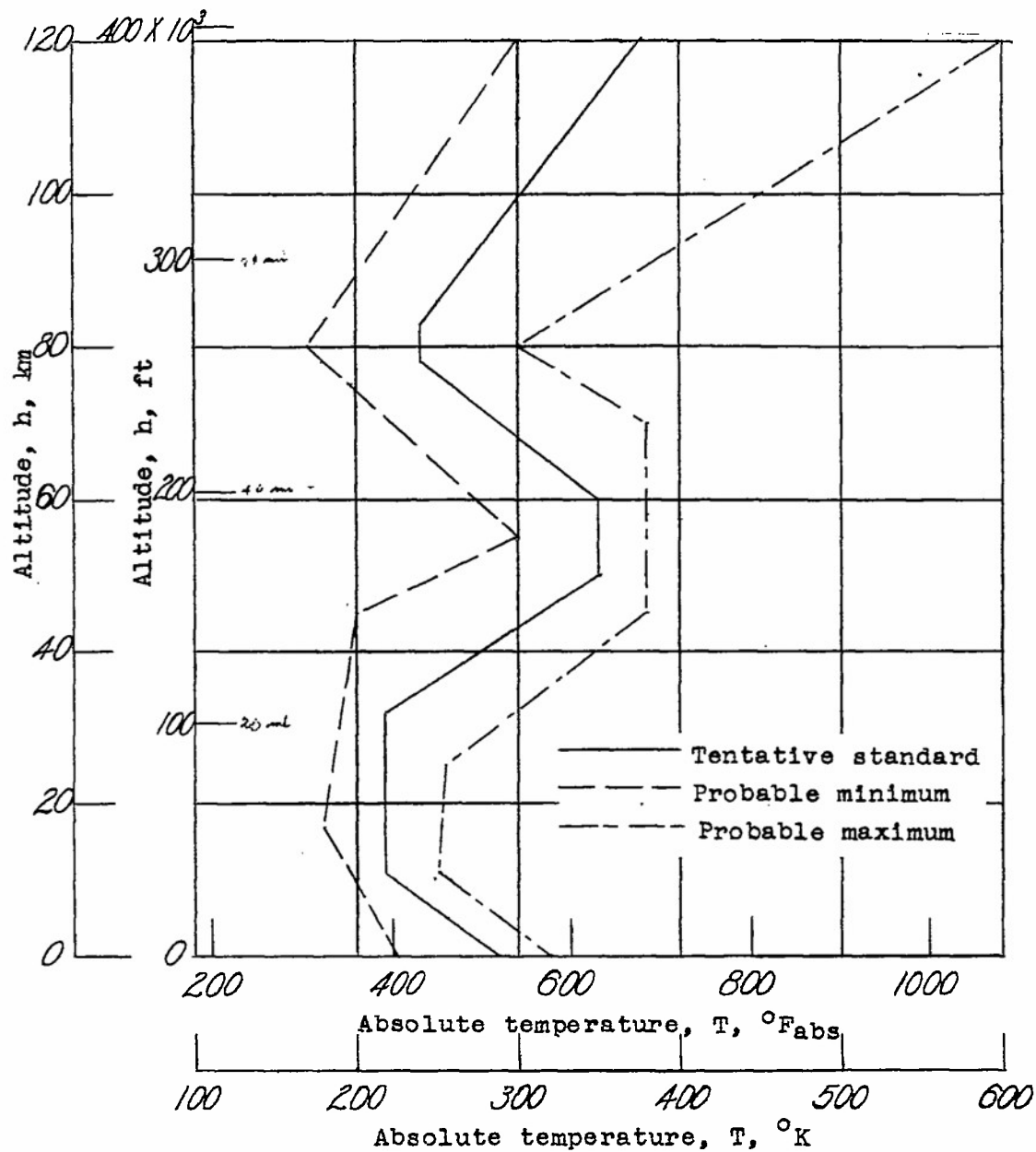
Altitude, h (ft)	Absolute tempera- ture, T (°F abs.)	Pressure, p (lb/ft <sup>2</sup> )	Pressure ratio, p/p <sub>0</sub>	Density, ρ (slugs/ft <sup>3</sup> )	Density ratio, ρ/ρ <sub>0</sub>	Specific weight, v = 62 (lb/ft <sup>3</sup> )	Coefficient of viscosity μ (lb-sec/ft <sup>2</sup> ) (1)	Kinematic viscosity, ν = μ/ρ (ft <sup>2</sup> /sec) (1)	Speed of sound, a (ft/sec)	Mean free path of molecules, λ (ft)
(c) For night only										
262,467	432.0	0.07527	3.557×10 <sup>-5</sup>	101.5×10 <sup>-9</sup>	4.268×10 <sup>-5</sup>	3.185×10 <sup>-6</sup>	3.212×10 <sup>-7</sup>	3.165	1019	5.53×10 <sup>-3</sup>
264,000	432.0	0.07051	3.332	95.07	3.998	2.983	3.212	3.379	1019	5.20
266,000	432.0	0.06480	3.062	87.36	3.674	2.741	3.212	3.677	1019	6.42
268,000	432.0	0.05955	2.814	80.30	3.377	2.519	3.212	4.000	1019	6.98
270,000	432.0	0.05473	2.586	73.79	3.103	2.314	3.212	4.353	1019	7.60
272,000	432.0	0.05032	2.378	67.87	2.854	2.128	3.212	4.732	1019	8.26
272,309	432.0	0.04955	2.346	66.94	2.815	2.099	3.212	4.795	1019	8.37
274,000	435.4	0.04622	2.184	61.83	2.600	1.938	3.232	5.227	1023	9.06
276,000	439.4	0.04252	2.009	56.36	2.370	1.766	3.257	5.779	1028	9.94
278,000	443.4	0.03913	1.849	51.41	2.162	1.611	3.282	6.384	1032	10.9
280,000	447.4	0.03604	1.703	46.92	1.973	1.470	3.306	7.046	1037	11.9
282,000	451.4	0.03320	1.569	42.85	1.802	1.342	3.331	7.774	1042	13.1
284,000	455.4	0.03066	1.449	39.21	1.649	1.228	3.355	8.551	1046	14.3
286,000	459.4	0.02832	1.338	35.92	1.510	1.124	3.379	9.401	1051	15.6
288,000	463.4	0.02618	1.237	32.91	1.384	1.030	3.403	10.34	1055	17.0
290,000	467.4	0.02423	1.145	30.20	1.270	0.9452	3.427	11.35	1060	18.5
292,000	471.4	0.02239	1.058	27.65	1.163	0.8654	3.451	12.48	1064	20.2
294,000	475.4	0.02072	0.9793	25.40	1.068	0.7949	3.475	13.68	1069	22.0
296,000	479.4	0.01919	0.9069	23.32	0.9806	0.7294	3.499	15.00	1073	24.0
298,000	483.4	0.01780	0.8409	21.44	0.9017	0.6706	3.523	16.43	1078	26.1
300,000	487.4	0.01653	0.7810	19.75	0.8306	0.6176	3.546	17.95	1082	28.3
302,000	491.4	0.01534	0.7247	18.18	0.7645	0.5683	3.569	19.53	1087	30.8
304,000	495.4	0.01424	0.6729	16.74	0.7041	0.5233	3.593	21.46	1091	33.4
306,000	499.4	0.01324	0.6255	15.44	0.6492	0.4824	3.616	23.42	1096	36.2
308,000	503.4	0.01231	0.5818	14.25	0.5991	0.4451	3.639	25.54	1100	39.2
310,000	507.4	0.01146	0.5414	13.15	0.5531	0.4109	3.662	27.84	1104	42.4
312,000	511.5	0.01067	0.5042	12.15	0.5110	0.3795	3.685	30.33	1109	46.0
314,000	515.5	0.009940	0.4697	11.23	0.4724	0.3508	3.708	33.02	1113	49.7
316,000	519.5	0.009265	0.4378	10.39	0.4369	0.3244	3.731	35.91	1117	53.7
318,000	523.5	0.008643	0.4084	9.616	0.4044	0.3002	3.754	39.04	1122	58.0
320,000	527.5	0.008061	0.3809	8.903	0.3744	0.2779	3.777	42.42	1126	62.7
322,000	531.5	0.007527	0.3557	8.251	0.3470	0.2575	3.799	46.04	1130	67.6
324,000	535.5	0.007028	0.3321	7.645	0.3215	0.2385	3.822	49.99	1134	73.0
326,000	539.5	0.006571	0.3105	7.096	0.2984	0.2213	3.844	54.17	1139	78.6
328,000	543.5	0.006146	0.2904	6.587	0.2770	0.2054	3.867	58.71	1143	84.6
330,000	547.5	0.005750	0.2717	6.118	0.2573	0.1908	3.889	63.57	1147	91.1
332,000	551.5	0.005379	0.2542	5.681	0.2389	0.1771	3.911	68.84	1151	98.1
334,000	555.5	0.005039	0.2381	5.284	0.2222	0.1647	3.933	74.43	1155	105
336,000	559.5	0.004721	0.2231	4.915	0.2067	0.1532	3.955	80.47	1160	113
338,000	563.5	0.004427	0.2092	4.577	0.1925	0.1426	3.977	86.91	1164	122
340,000	567.5	0.004152	0.1962	4.261	0.1792	0.1327	3.999	93.85	1168	131
342,000	571.5	0.003892	0.1839	3.966	0.1668	0.1235	4.021	101.4	1172	140
344,000	575.5	0.003655	0.1727	3.700	0.1556	0.1152	4.043	109.3	1176	150
344,487	576.5	0.003602	0.1702	3.638	0.1530	0.1134	4.048	111.2	1177	153
346,000	579.5	0.003433	0.1623	3.429	0.1442	0.1068	4.065	118.5	1185	161
348,000	583.5	0.003231	0.1527	3.179	0.1337	0.09896	4.086	128.5	1195	172
350,000	587.5	0.003041	0.1437	2.946	0.1239	0.09169	4.108	139.5	1205	184
352,000	591.5	0.002863	0.1353	2.732	0.1149	0.08502	4.129	151.1	1215	197
354,000	595.5	0.002700	0.1276	2.537	0.1067	0.07893	4.151	163.6	1226	211
356,000	599.5	0.002546	0.1203	2.358	0.09916	0.07334	4.172	176.9	1236	225
358,000	603.5	0.002404	0.1136	2.194	0.09227	0.06823	4.193	191.1	1246	240
360,000	607.5	0.002273	0.1074	2.044	0.08597	0.06356	4.214	206.2	1256	255
362,000	611.5	0.002150	0.1016	1.906	0.08015	0.05925	4.236	222.2	1266	271
364,000	615.5	0.002035	0.09614	1.778	0.07476	0.05525	4.257	239.4	1277	288
366,000	619.6	0.001928	0.09111	1.661	0.06984	0.05161	4.278	257.6	1287	306
368,000	623.6	0.001828	0.08639	1.553	0.06529	0.04824	4.299	276.8	1297	325
370,000	627.6	0.001736	0.08201	1.453	0.06111	0.04514	4.319	297.2	1308	345
372,000	631.6	0.001649	0.07790	1.361	0.05724	0.04227	4.340	318.9	1318	365
374,000	635.6	0.001567	0.07405	1.276	0.05366	0.03966	4.361	341.6	1328	386
376,000	639.6	0.001489	0.07038	1.197	0.05033	0.03716	4.382	365.1	1339	409
378,000	643.6	0.001417	0.06698	1.123	0.04722	0.03485	4.402	392.0	1349	433
380,000	647.6	0.001350	0.06379	1.055	0.04436	0.03274	4.423	419.2	1360	457
382,000	651.6	0.001286	0.06079	0.9916	0.04170	0.03077	4.443	448.0	1370	482
384,000	655.6	0.001227	0.05797	0.9331	0.03924	0.02895	4.464	478.4	1381	509
386,000	659.6	0.001170	0.05531	0.8784	0.03694	0.02725	4.484	510.5	1391	536
388,000	663.6	0.001118	0.05282	0.8277	0.03481	0.02567	4.504	544.2	1401	565
390,000	667.6	0.001068	0.05045	0.7804	0.03282	0.02420	4.525	579.8	1412	595
392,000	671.6	0.001020	0.04823	0.7364	0.03097	0.02282	4.545	617.2	1422	626
393,700	675.0	0.0009830	0.04645	0.7015	0.02950	0.02173	4.562	650.4	1431	653

<sup>1</sup>The values for viscosity listed in these columns are not applicable at the higher altitudes where the mean free paths of the molecules are comparable to or longer than the dimensions of the body being considered. Furthermore, the values listed are based on the conventional Sutherland formula for normal air and, consequently, no allowance has been made for the effect of dissociated oxygen in the atmosphere at the higher levels.

TABLE VI.- LATITUDE CORRECTION FACTORS FOR VALUES OF PRESSURE IN TABLES IV AND V

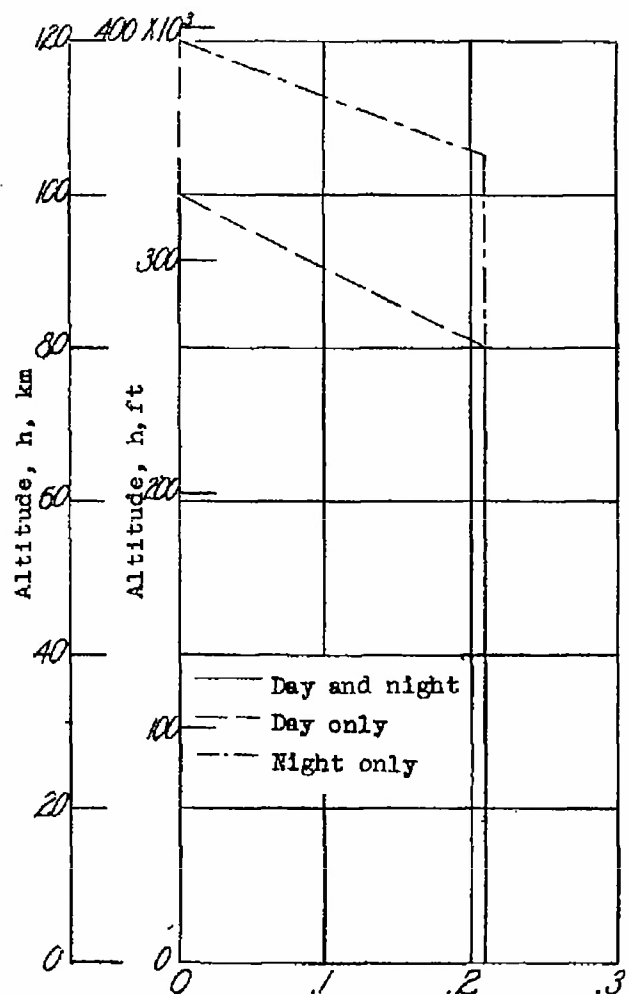
Latitude, deg											
Altitude, h'		0	10	20	30	40	50	60	70	80	90
(km)	(ft)										
(a) For both day and night											
20	65,617	1.0078	1.0073	1.0060	1.0039	1.0014	0.9988	0.9963	0.9943	0.9929	0.9925
30	98,425	1.0120	1.0112	1.0092	1.0060	1.0022	.9981	.9943	.9912	.9892	.9885
40	131,233	1.0158	1.0148	1.0121	1.0080	1.0029	.9975	.9925	.9884	.9858	.9848
50	164,042	1.0187	1.0176	1.0144	1.0094	1.0034	.9971	.9911	.9863	.9832	.9821
60	196,850	1.0213	1.0200	1.0154	1.0108	1.0039	.9967	.9899	.9844	.9808	.9796
70	229,658	1.0242	1.0227	1.0186	1.0122	1.0044	.9962	.9886	.9824	.9783	.9769
80	262,467	1.0278	1.0260	1.0212	1.0140	1.0051	.9957	.9869	.9798	.9752	.9736
(b) For day only											
80	262,467	1.0278	1.0260	1.0212	1.0140	1.0051	0.9957	0.9869	0.9798	0.9752	0.9736
90	295,275	1.0312	1.0293	1.0239	1.0157	1.0057	.9952	.9853	.9774	.9722	.9704
100	328,083	1.0340	1.0319	1.0261	1.0171	1.0062	.9947	.9840	.9754	.9698	.9679
110	360,892	1.0364	1.0342	1.0279	1.0183	1.0066	.9944	.9830	.9738	.9678	.9657
120	393,700	1.0385	1.0361	1.0295	1.0193	1.0070	.9940	.9820	.9723	.9660	.9638
(c) For night only											
80	262,467	1.0278	1.0260	1.0212	1.0140	1.0051	0.9957	0.9869	0.9798	0.9752	0.9736
90	295,275	1.0314	1.0295	1.0241	1.0158	1.0057	.9951	.9852	.9772	.9721	.9703
100	328,083	1.0346	1.0325	1.0265	1.0174	1.0063	.9946	.9838	.9750	.9693	.9673
110	360,892	1.0374	1.0352	1.0287	1.0188	1.0068	.9942	.9825	.9730	.9669	.9647
120	393,700	1.0397	1.0373	1.0304	1.0199	1.0072	.9938	.9815	.9714	.9649	.9627

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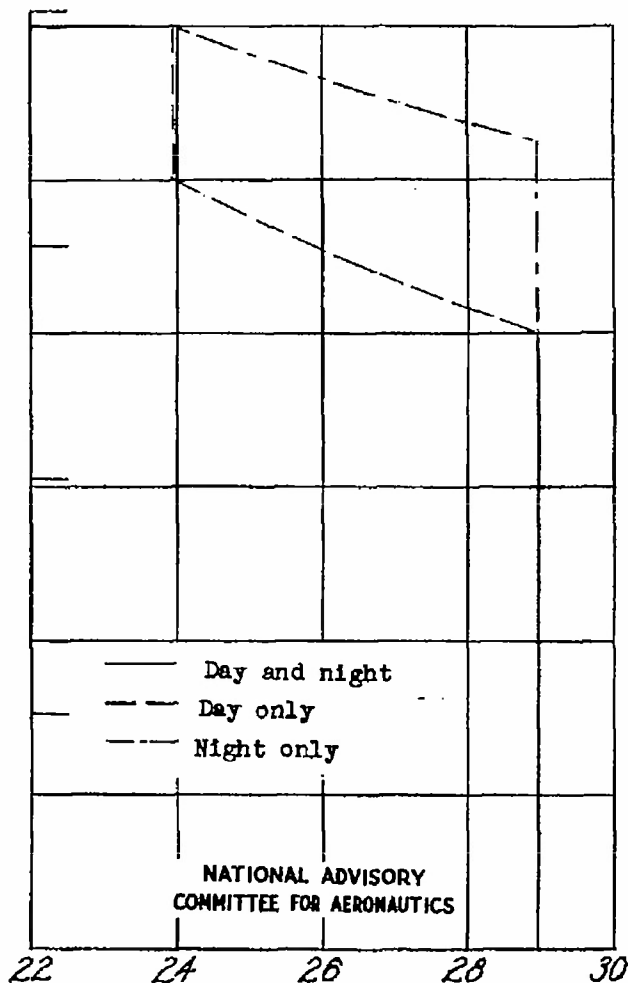


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Figure 1.- Variation of ambient temperature with altitude.

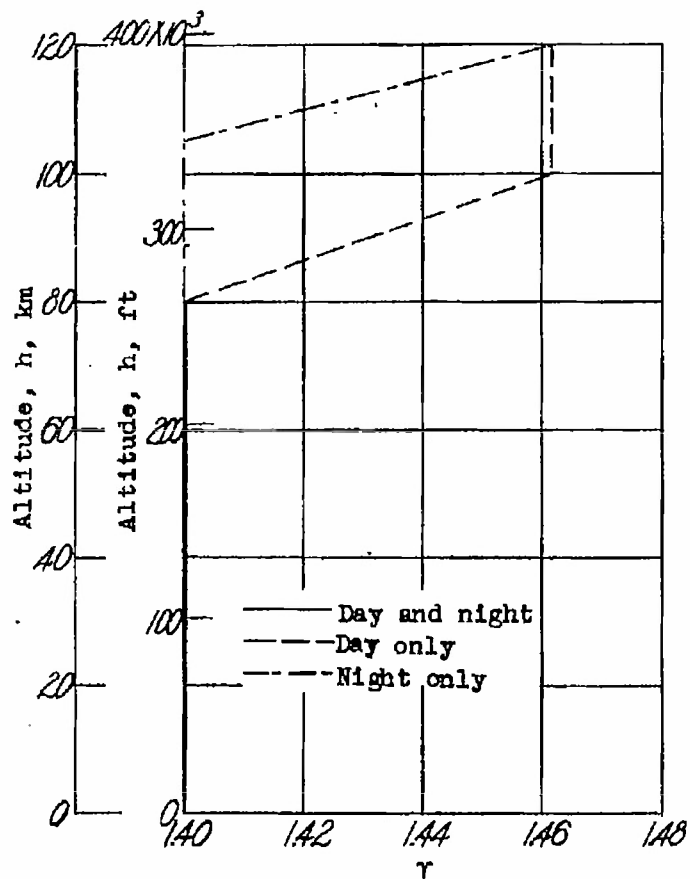


(a) Relative volume of molecular oxygen,  $v_m$ .



(b) Average molecular weight,  $M$ .

Figure 2.- Variation of composition of the tentative standard atmosphere with altitude. (The dissociation of oxygen is the only change in composition occurring in the tentative standard atmosphere.)



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(a) Ratio of specific heats,  $\gamma$ .

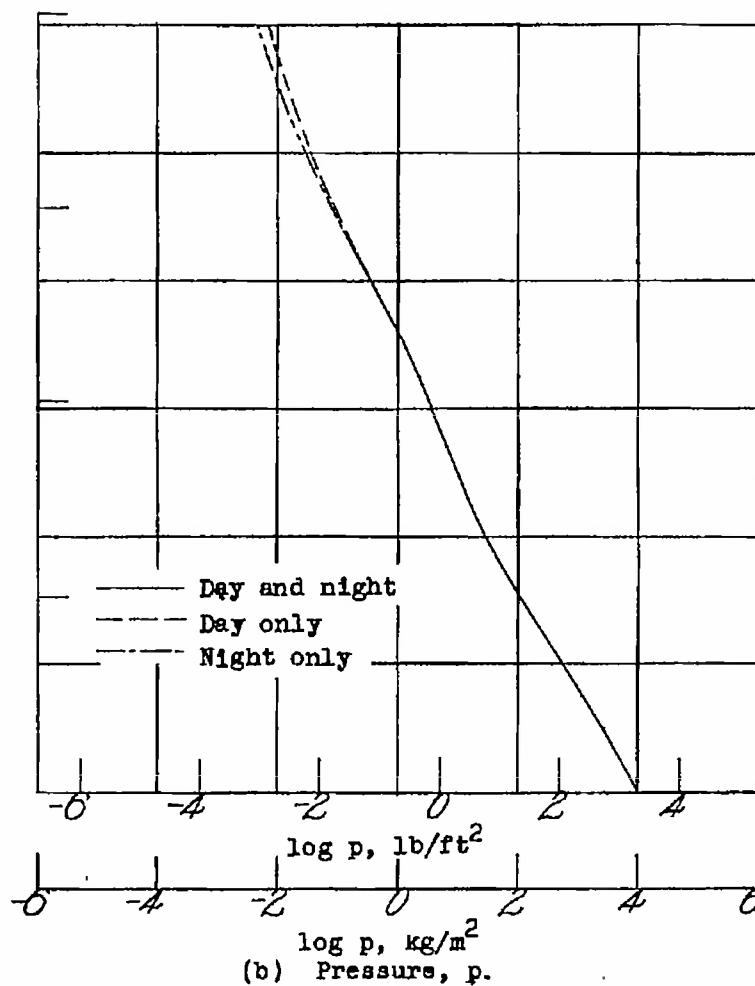


Figure 3. Variation with altitude of the physical properties of the tentative standard atmosphere.

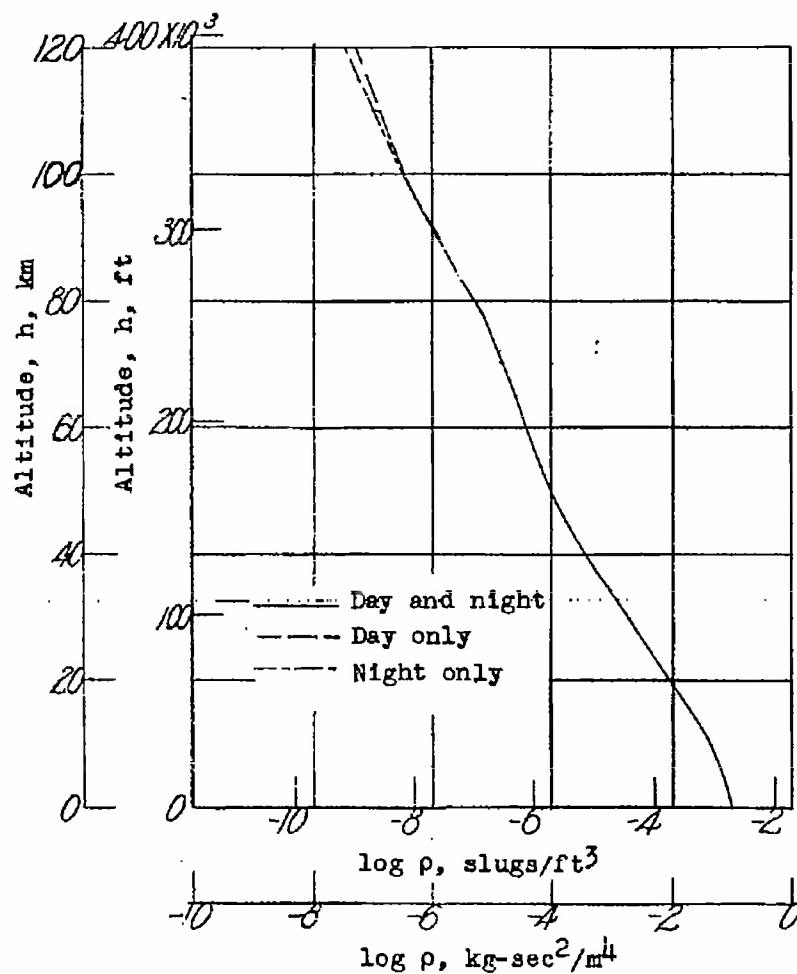
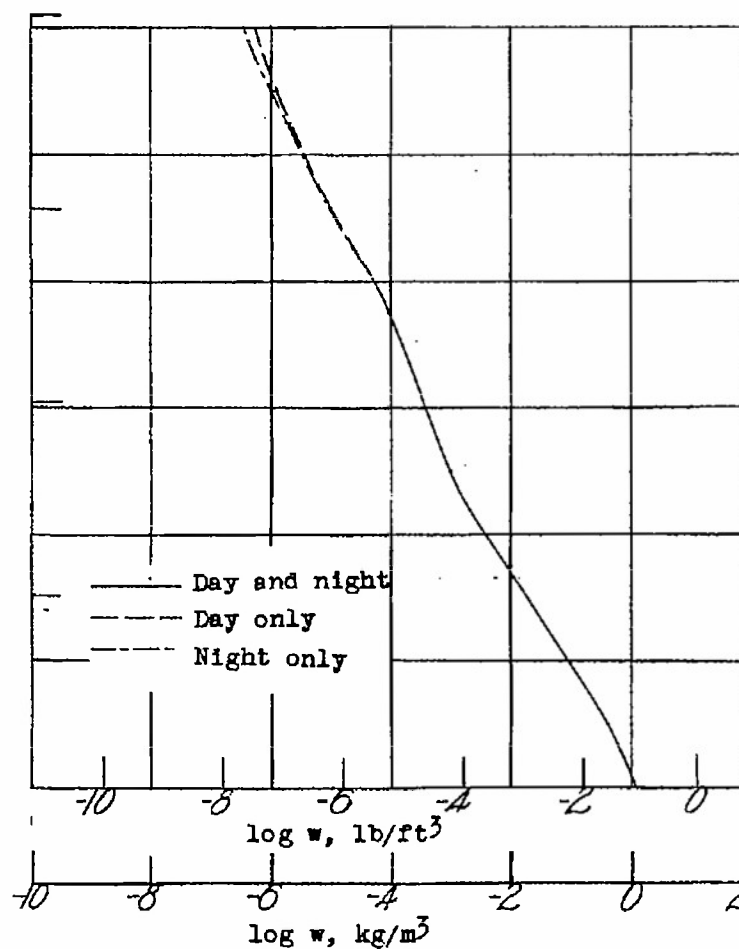
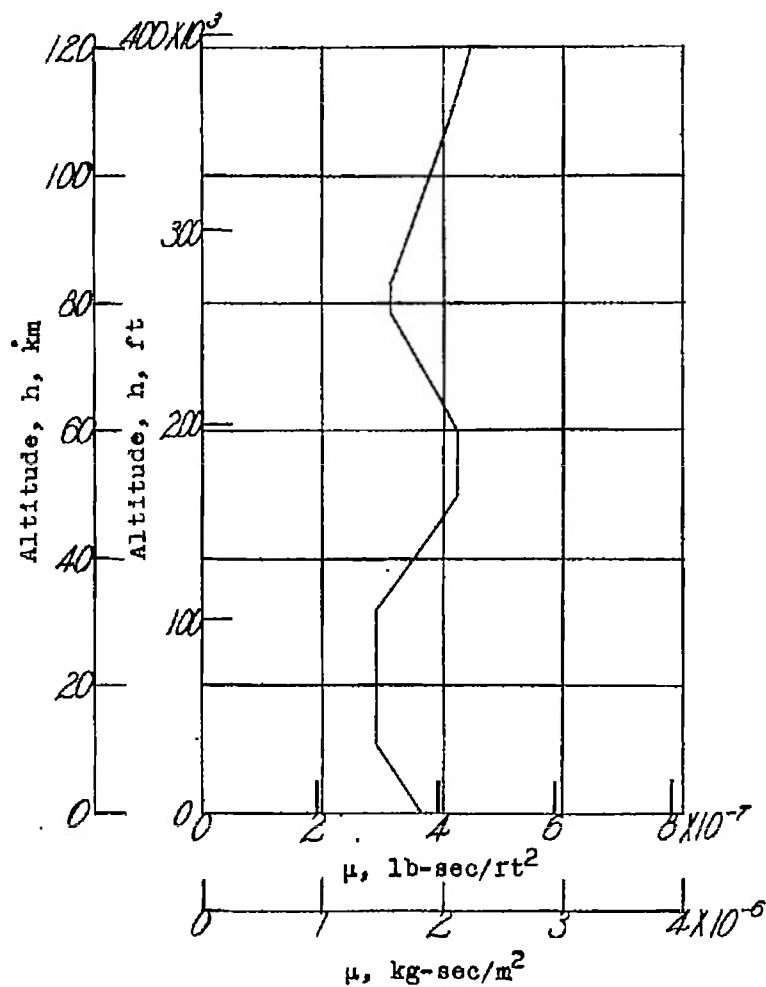
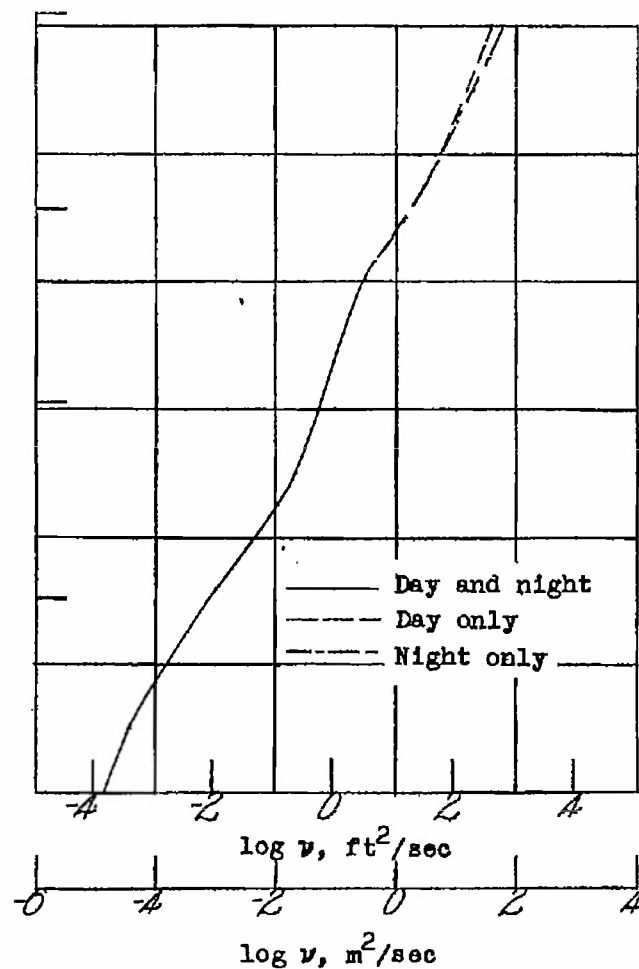
(c) Density,  $\rho$ .(d) Specific weight,  $w$ .

Figure 3.- Continued.

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(e) Coefficient of viscosity,  $\mu$ .



(f) Kinematic viscosity,  $\nu$ .

Figure 3.- Continued.

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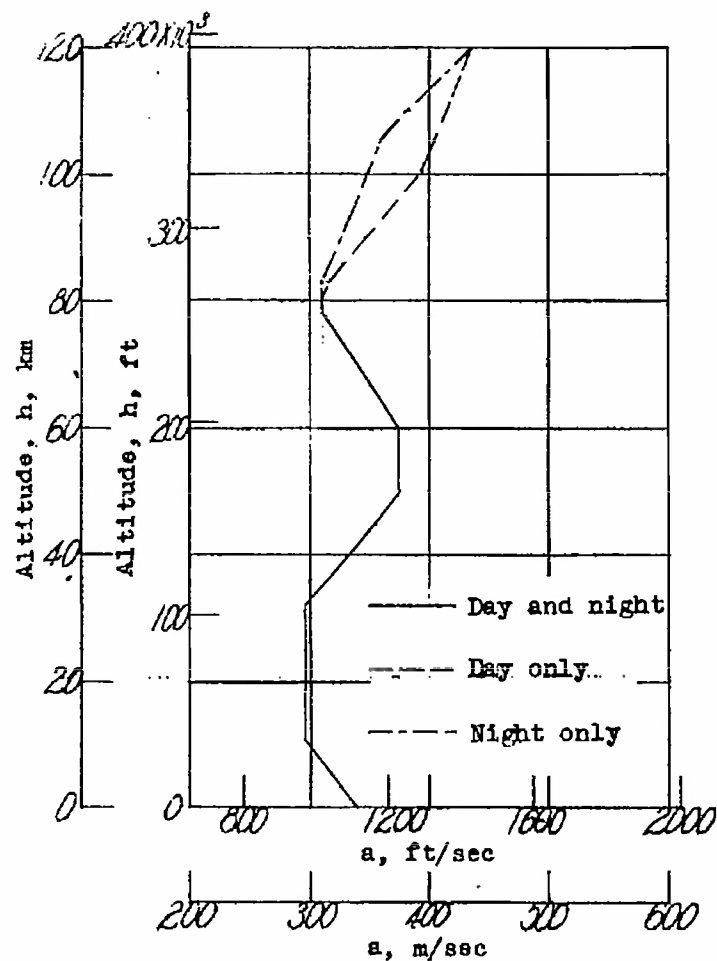
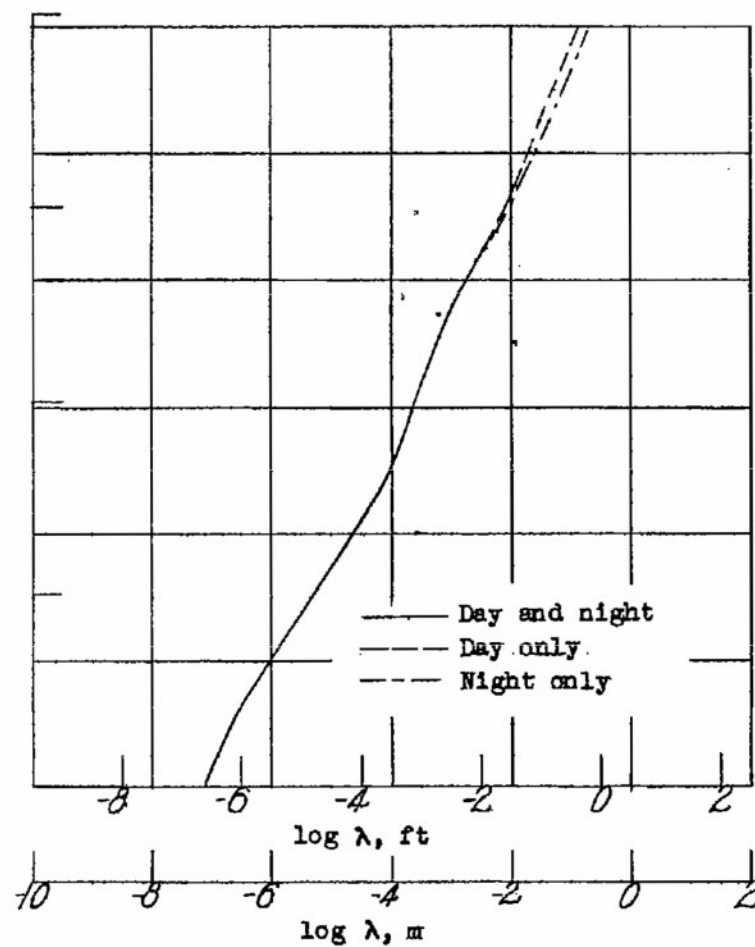
(g) Speed of sound,  $a$ .(h) Mean free path of molecules,  $\lambda$ .

Figure 3.- Concluded.

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Jan ' 47	Unclass.	U. S.	English	56	tables, graphs

**ABSTRACT:**

Two sets of tables based upon tentative standard specifications for the upper atmosphere are presented. One set constitutes a consistent extension of the standard tables for the lower atmosphere. The other set takes into consideration the decrease in the acceleration of gravity with increasing altitude and, therefore, is more precise than the first set. All quantities listed in the tables against altitude are computed from adopted temperature-height and composition-height relationships.

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**DIVISION:** Meteorology (30)

**SECTION:** Upper Air Research (3)

**SUBJECT HEADINGS:** Meteorology, Upper air (62000); Atmosphere, Upper - Research (12398); Atmospheric tables (12440)

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